

# ISOLDE: laser ion source

Nuclear shape coexistence  
via  $\alpha$ - and  $\beta$ -decay studies with the  
application of the laser ion source

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# *Windmill-ISOLTRAP-RILIS* *collaboration*

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**IS 456, 466, 511, 534, 598, 608**

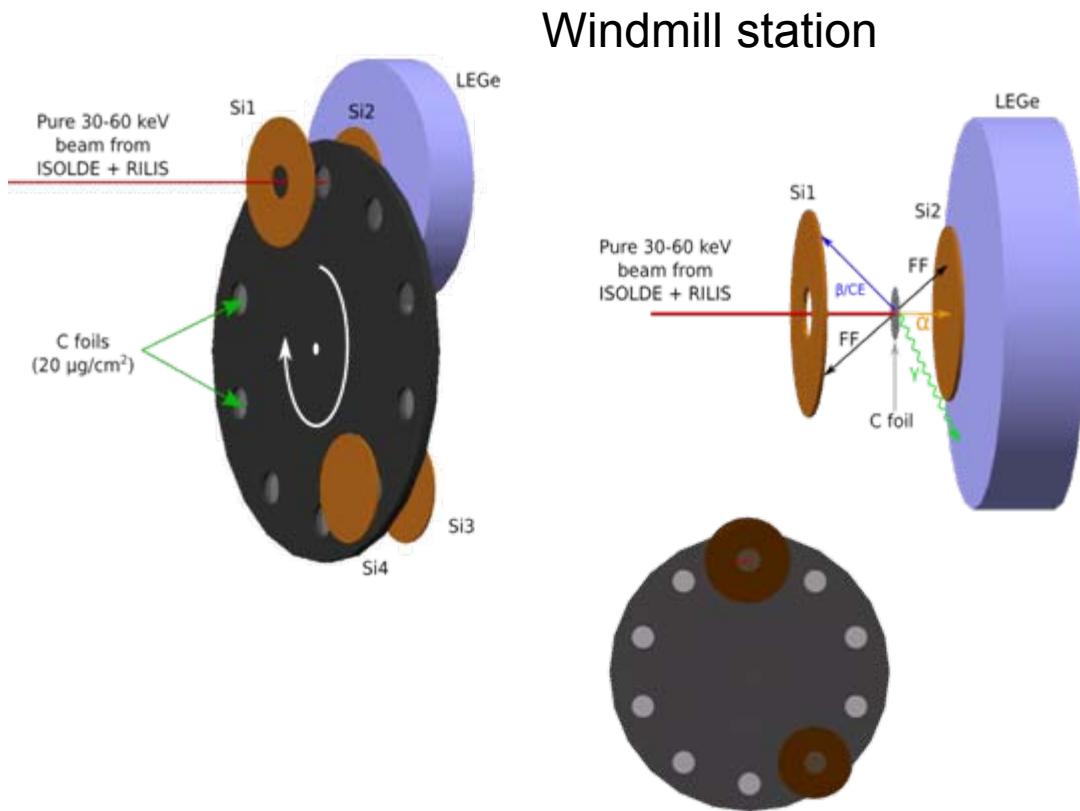
# $\alpha$ - and $\beta$ -decay studies at Windmill

## Main information:

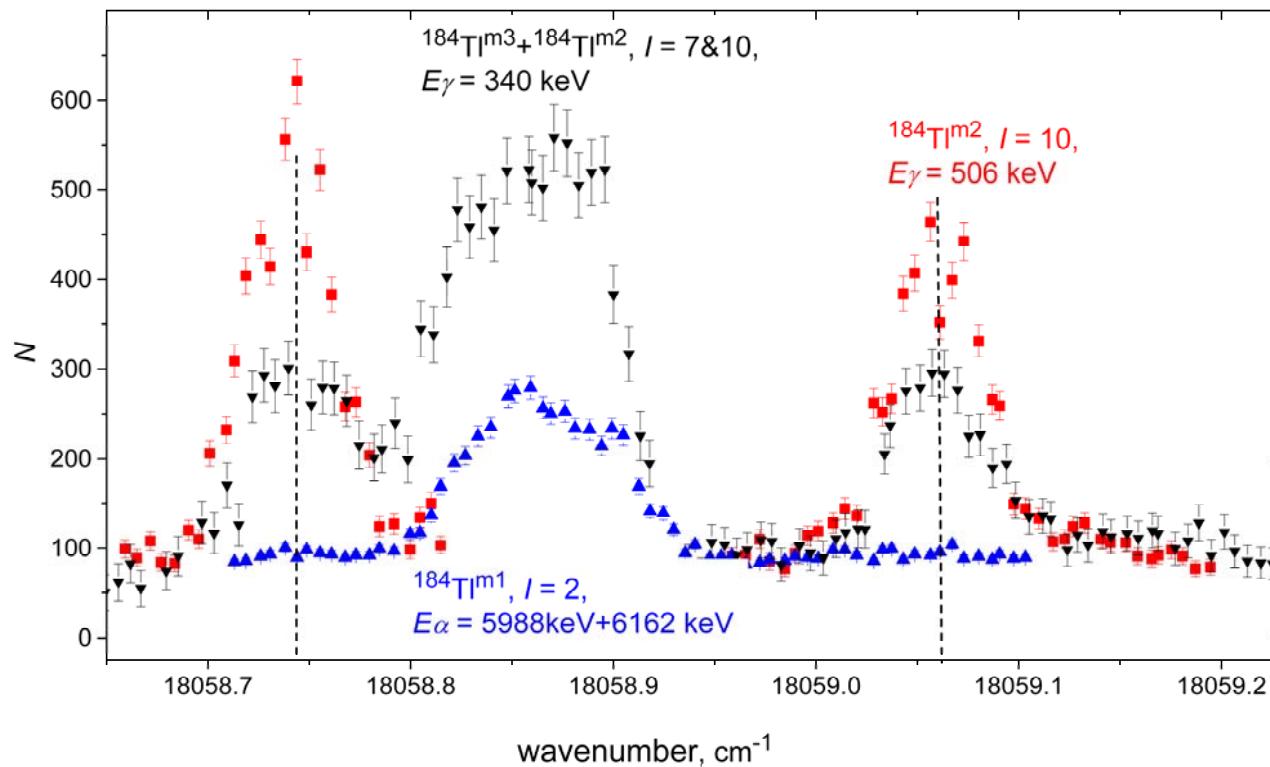
$I$ ,  $\delta\langle r^2 \rangle$ ,  $\mu$ ,  $Q$

## Additional information:

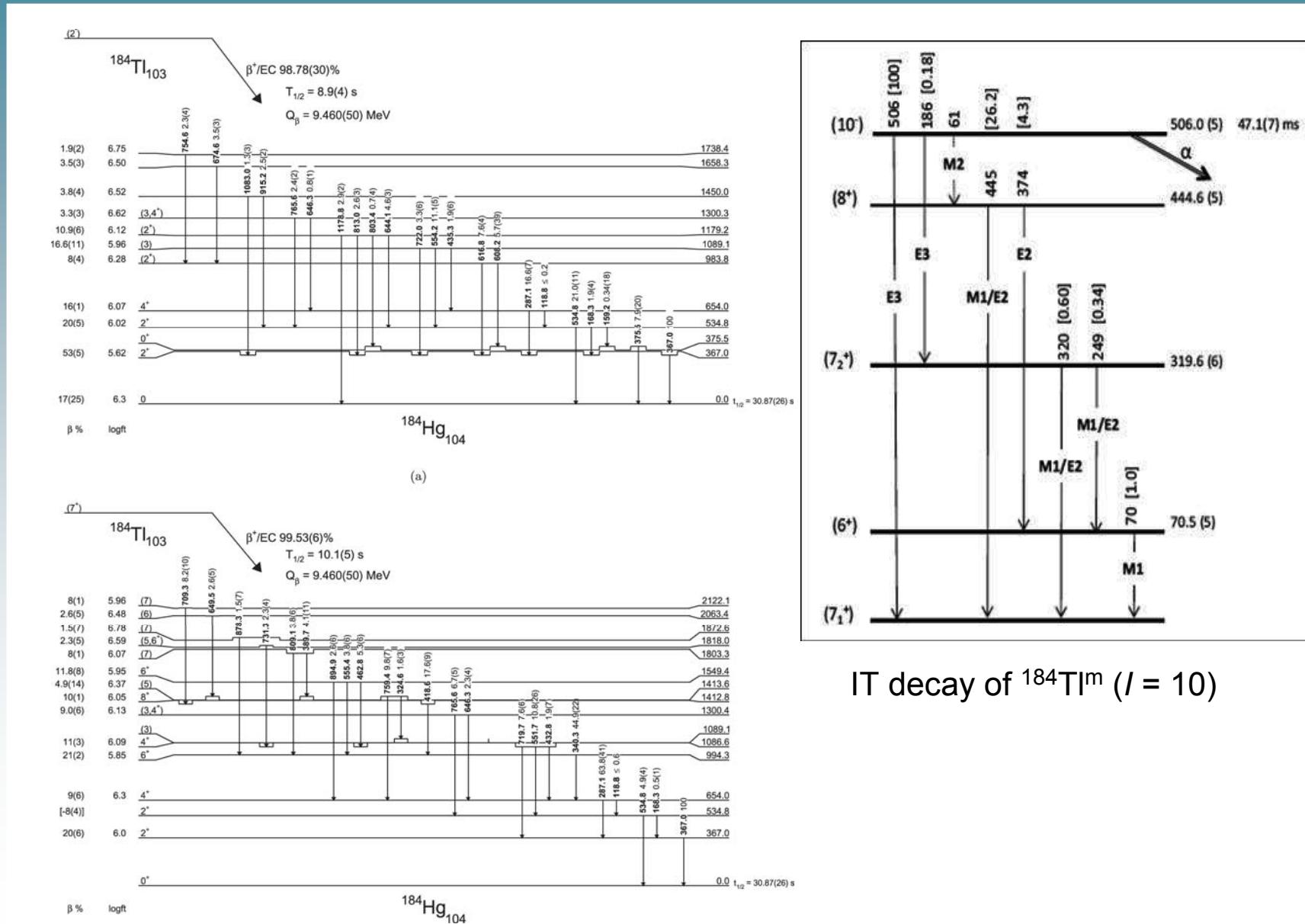
$T_{1/2}$   
 $E_\alpha$ ,  $b_\alpha$ ,  $b_\beta$   
 $Q_\alpha$  (masses)  
 $\alpha$ - $\gamma$ ,  $\gamma$ - $\gamma$  coincidence  
levels,  $E_\gamma$   
hindrance factors  
transition multipolarities  
conversion coefficients  
 $E0$  transitions  
partial decay schemes  
(isomer selectivity)



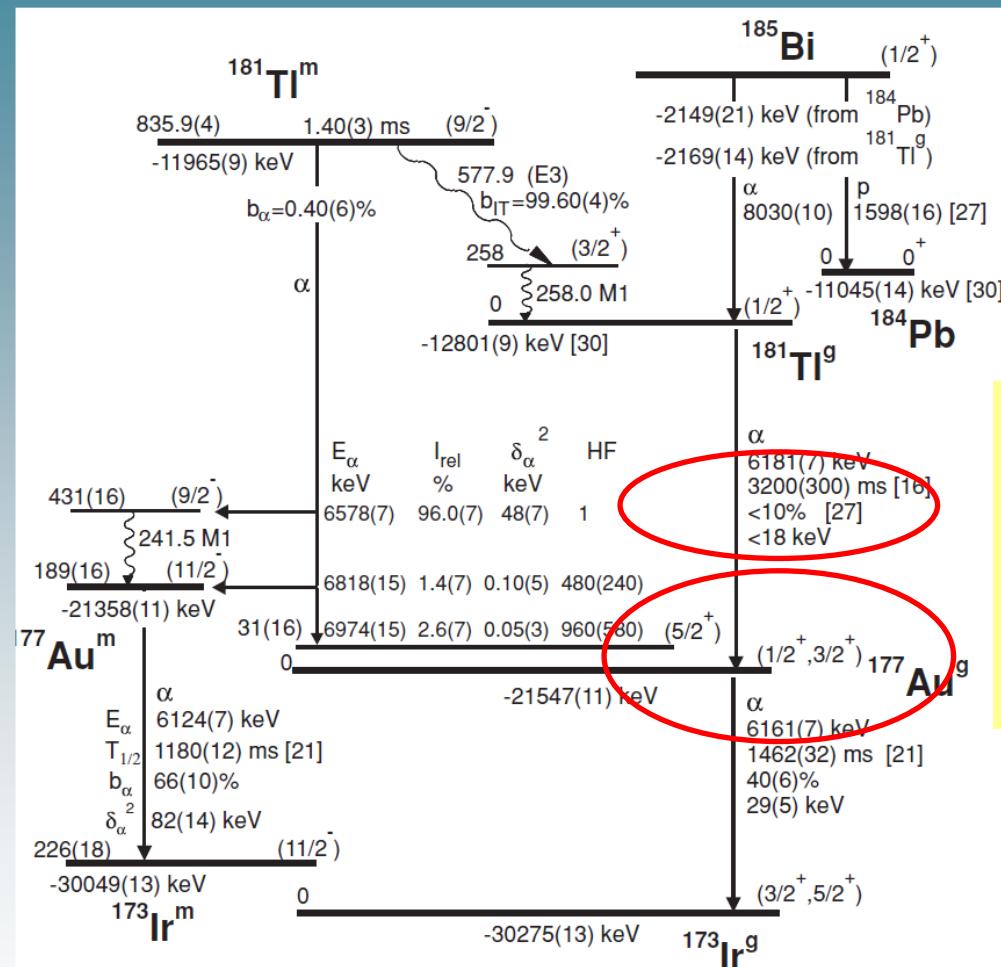
# Isomer selective $\alpha$ and $\beta$ decays



# Isomer selective $\alpha$ and $\beta$ decays



# Hindered $\alpha$ decay $^{181}\text{Tl} \rightarrow ^{177}\text{Au}$

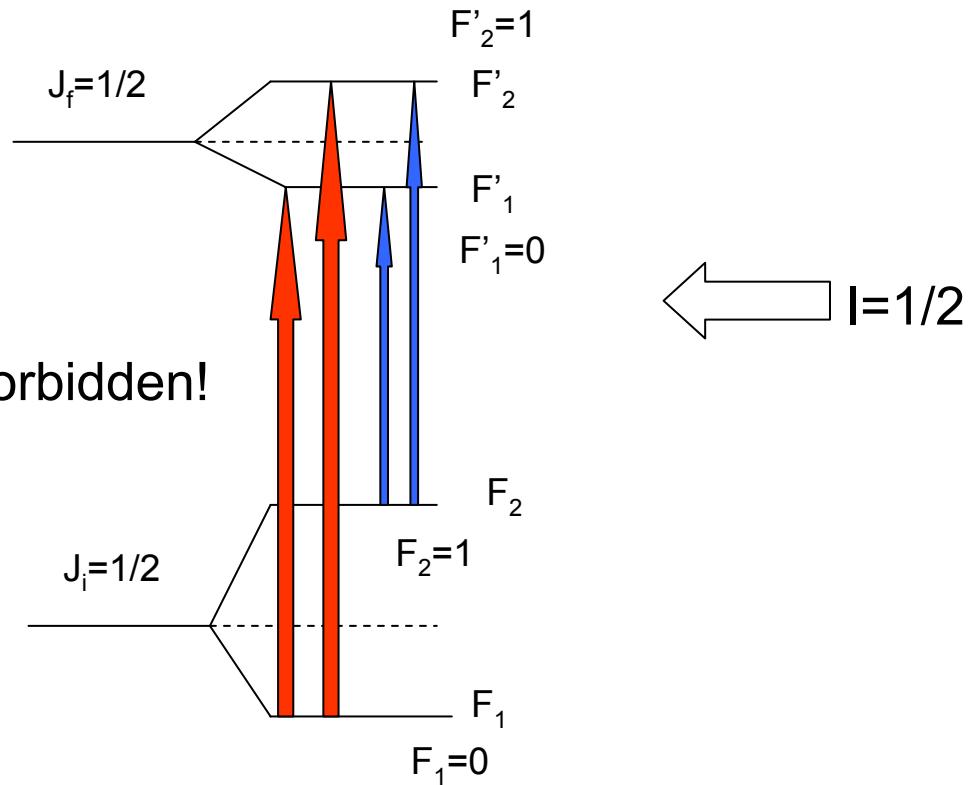


$$\delta_\alpha^2 = \frac{b_\alpha \ln(2)}{T_{1/2}} \frac{h}{P},$$

$$P = \exp \left[ -2 \int_{R_i}^{R_o} \frac{2\mu^{1/2}}{h} (V - Q_\alpha)^{1/2} dr \right]$$

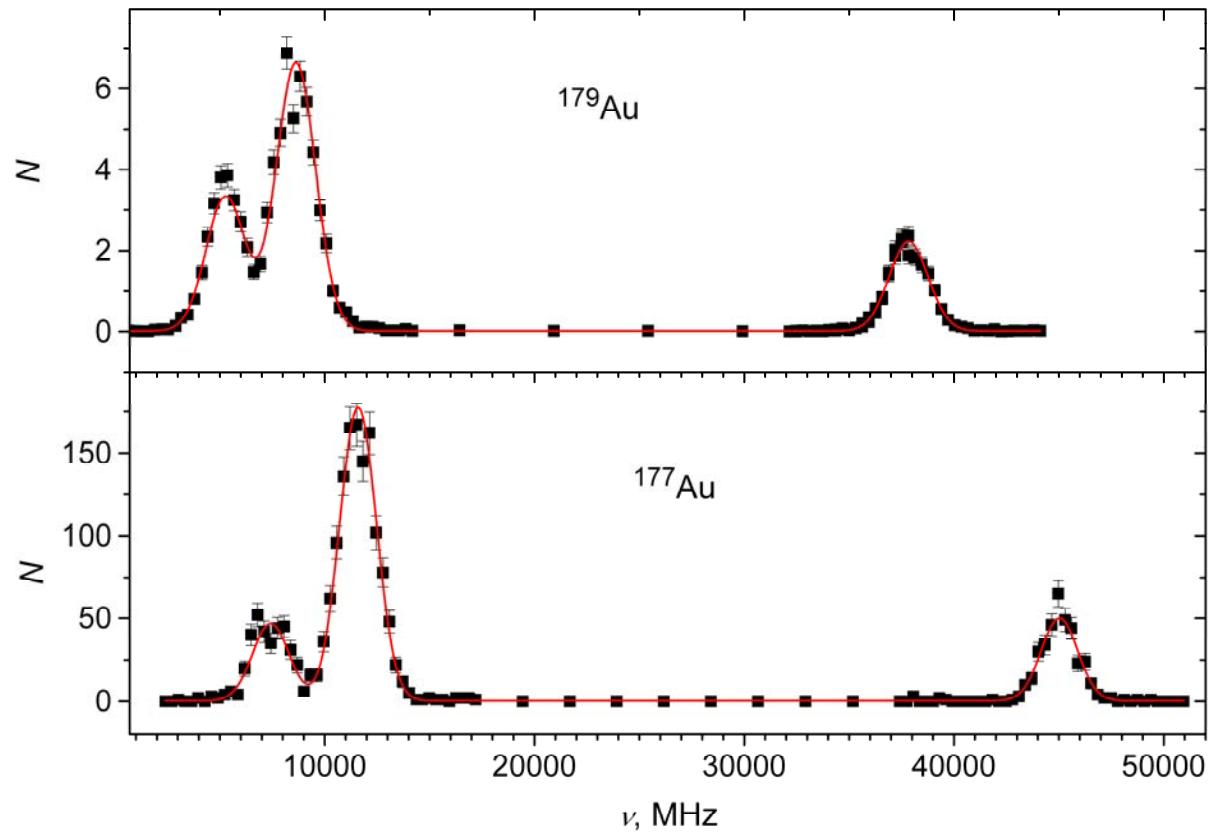
Why is  $\alpha$  decay of  $1/2^+$  gs of  $^{181}\text{Tl}$  hindered, HF>3?  
Different spins:  $^{181}\text{Tl}$  ( $1/2^+$ ) and  $^{177}\text{Au}$  ( $3/2^+$ )?

# Spins of $^{177}, ^{179}\text{Au}$



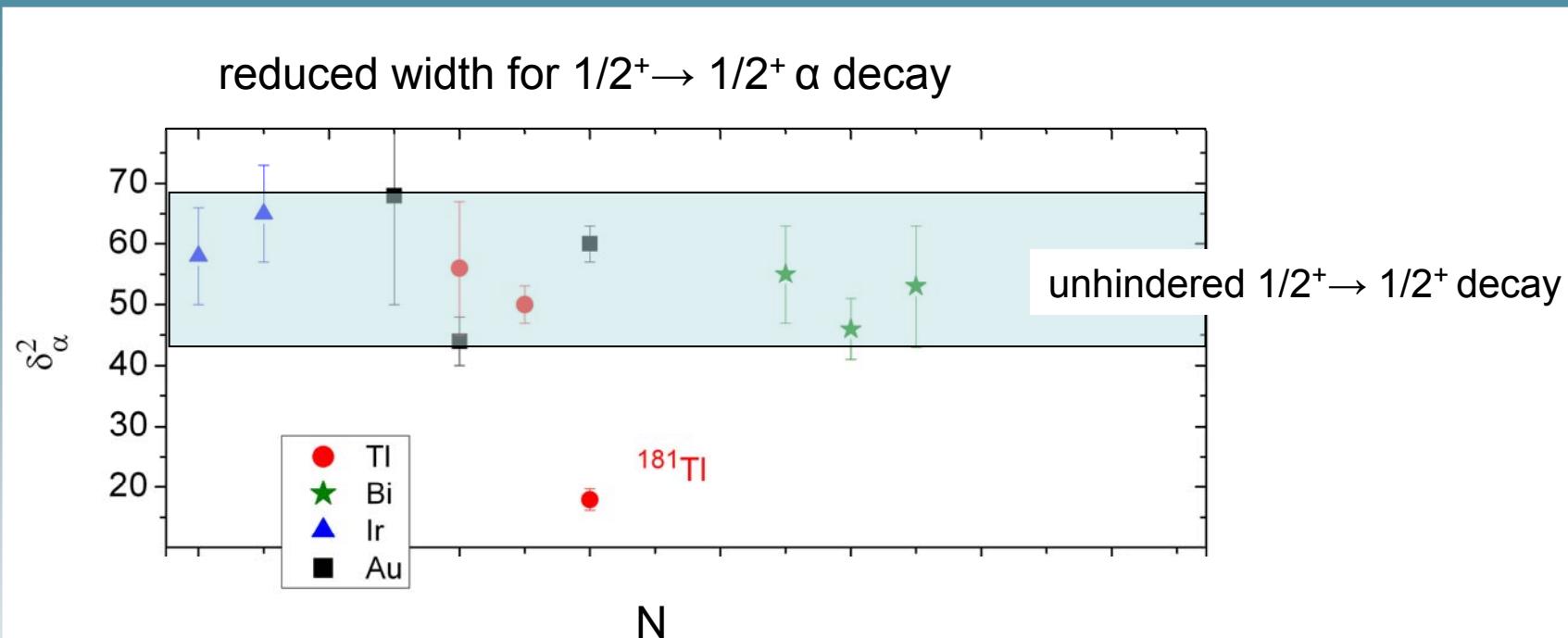
Only 3 rather than usual 4 lines will be seen in the hfs spectra  
of isotopes with  $I=1/2$

# Spins of $^{177}, ^{179}\text{Au}$

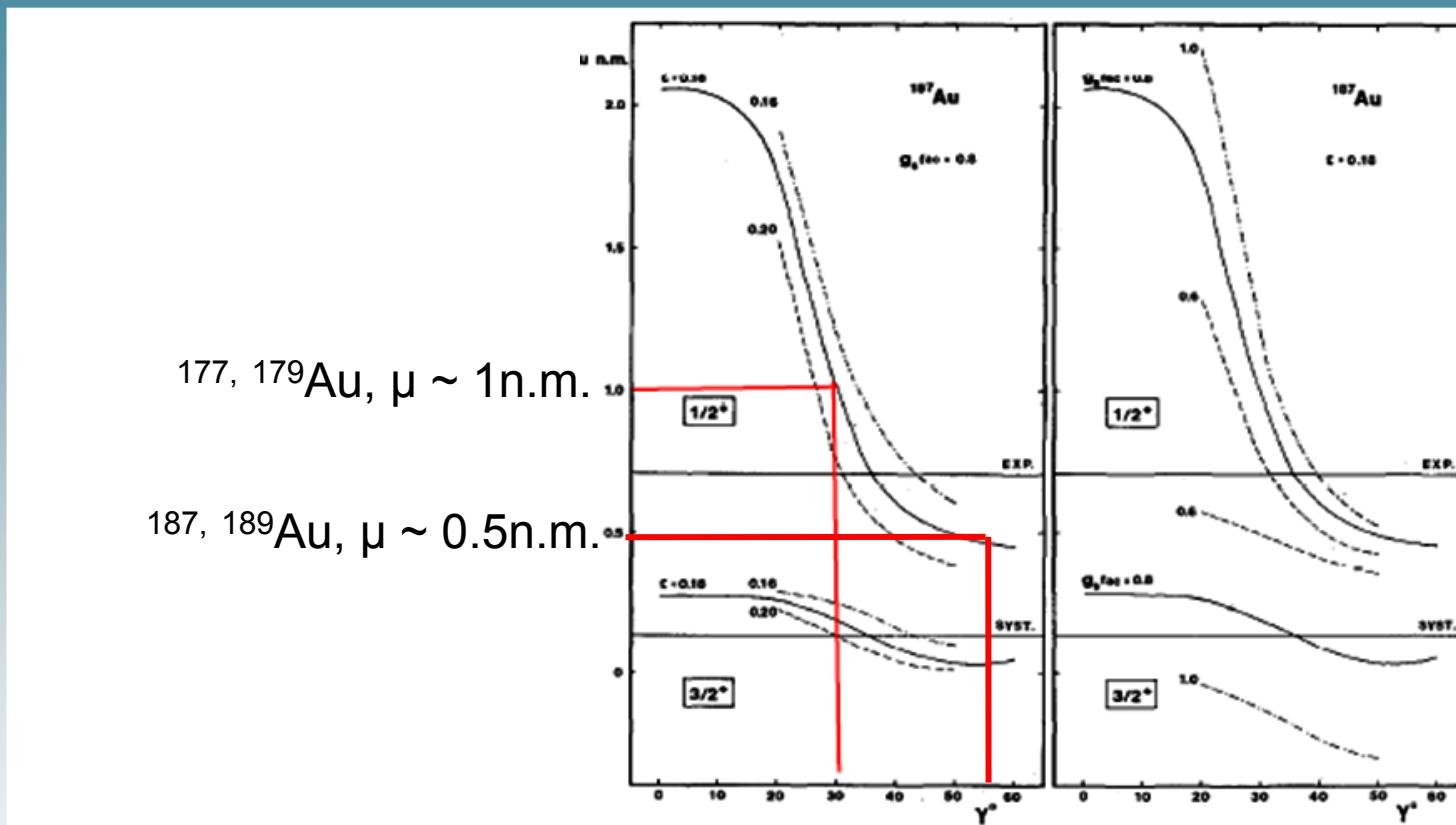


$$I(^{177,179}\text{Au}) = 1/2$$

# Hindrance factors and $\mu$

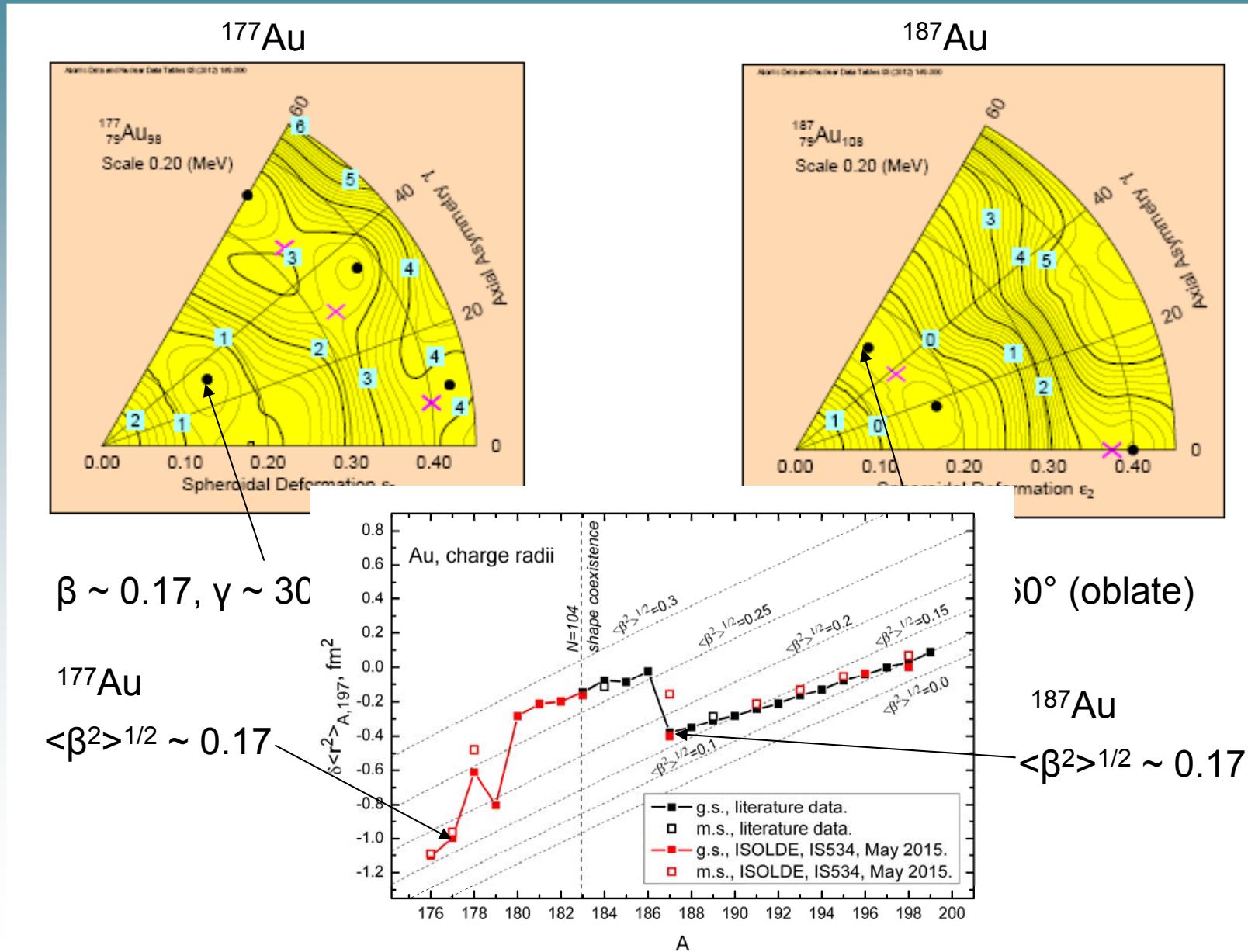


# Nonaxiality in $^{177}, ^{179}\text{Au}$

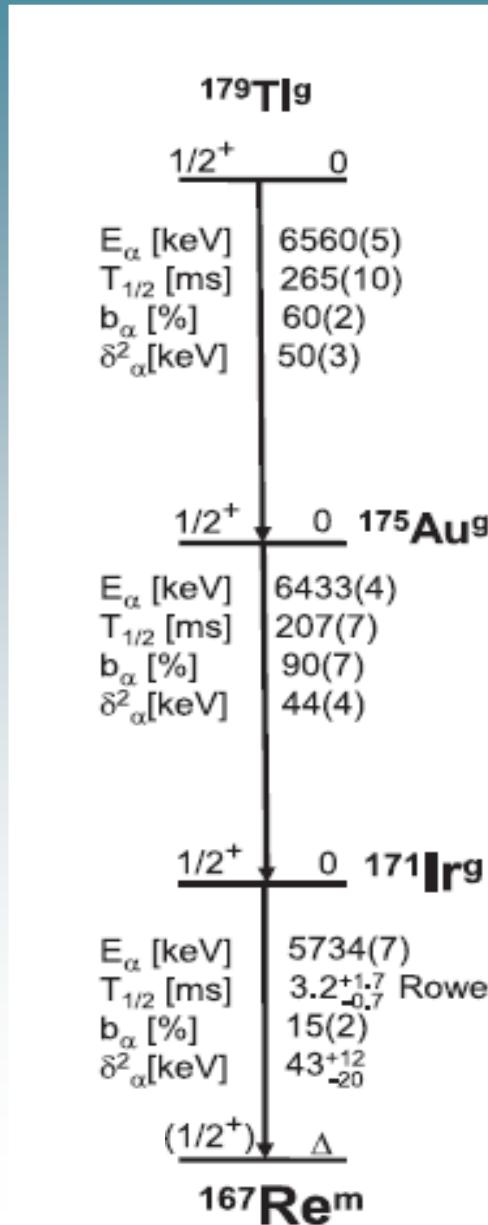


Thus, the structures of  $1/2^+$  states in parent  $^{181}\text{TI}$  and daughter  $^{177}\text{Au}$  are different: spherical  $s_{1/2}$  state in  $^{181}\text{TI}$  and nonaxially deformed mixture of  $s_{1/2}$  and  $d_{3/2}$  states in  $^{177}\text{Au} \rightarrow$  hindrance of the  $\alpha$  decay

# Potential energy surface calculations



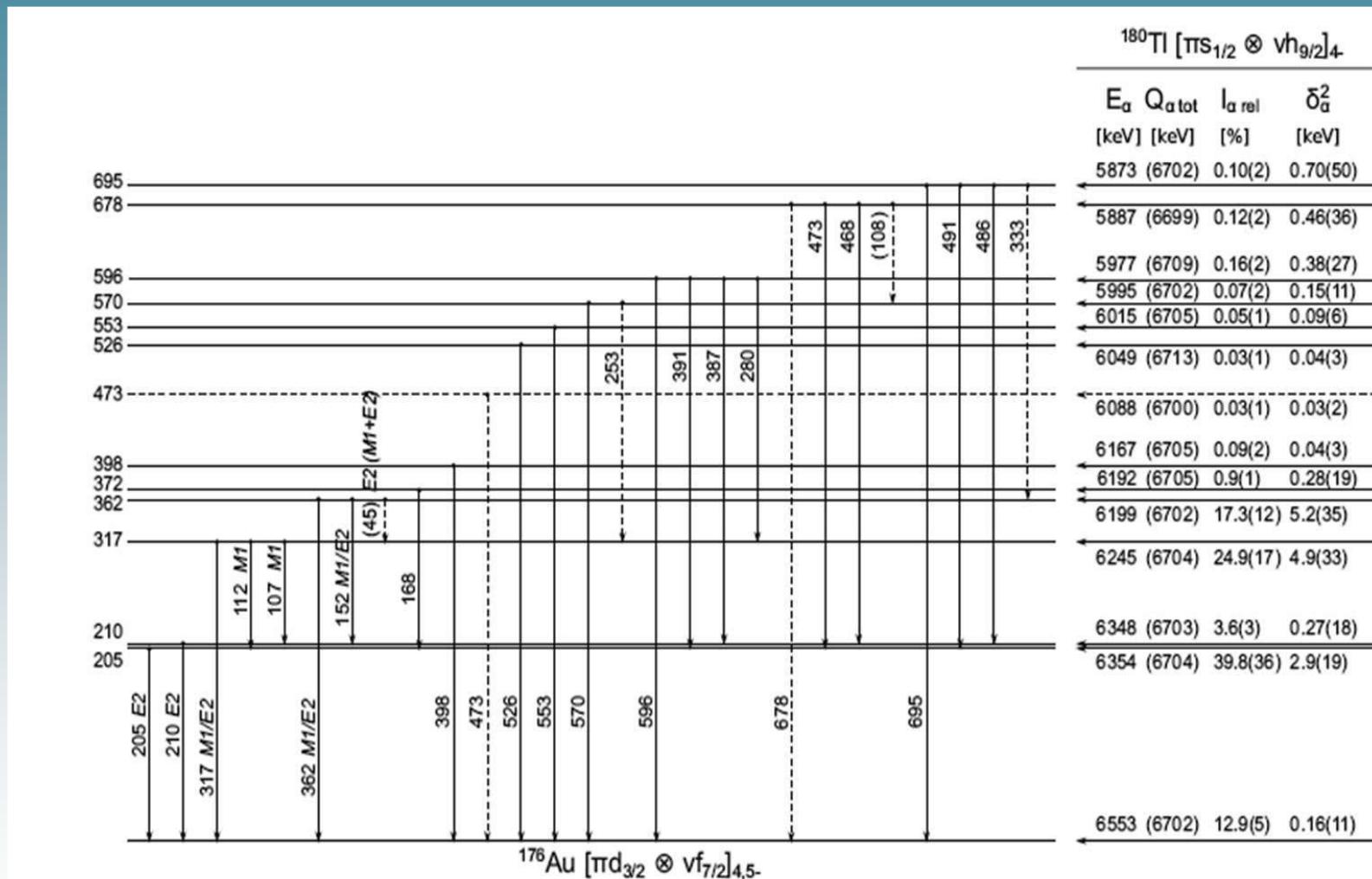
# Unhindered $\alpha$ decay of $^{179}\text{Tl}$



Unhindered  $\alpha$  decays point to the pure  $s_{1/2}$  configuration in all these nuclei.

The measurement of  $\mu(^{175}\text{Au})$  is needed to confirm this interpretation

# Large hindrance of $\alpha$ decay $^{180}\text{Tl}^g \rightarrow ^{176}\text{Au}^g$



# Large hindrance of $\alpha$ decay $^{180}\text{Tl}g \rightarrow ^{176}\text{Au}g$

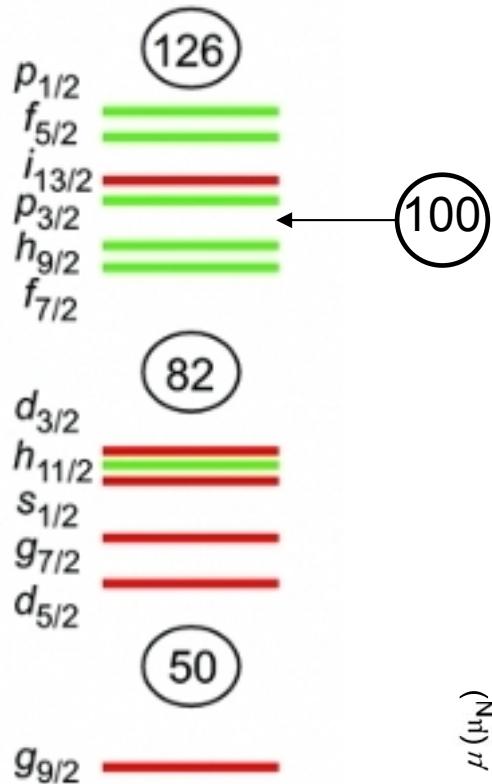
$^{178}\text{TI}$		$^{180}\text{TI}$		$^{182}\text{TI}$		$^{184}\text{TI}$	
$E_\alpha$ (keV)	$\delta^2$ (keV)						
<b>6862(10)</b>	<b>0.30(15)</b>	<b>6553(7)</b>	<b>0.16(11)</b>	6406	0.043(25)	6161	0.57(6)
6693(10)	13.0(17)	6354(7)	2.9(19)	6360(6)	0.048(28)	5988(12)	2.4(4)
6595(10)	10.2(24)	6348(7)	0.27(18)	6165(6)	1.13(66)	5964(12)	
		6245(7)	4.9(33)	6046(5)	5.8(34)	5810(12)	0.9(1)
		6199(7)	5.2(35)	5962(5)	6.0(35)	5748(12)	< 0.09

Strongly hindered  $gs \rightarrow gs$  decay ( $\delta^2 \sim 0.1$  keV; HF  $\sim 500$ ) at the same spin and deformation! Large hindrance is due to the change of both proton,  $s_{1/2} \rightarrow d_{3/2}$ , and neutron,  $h_{9/2} \rightarrow f_{7/2}$ , configurations (confirmed by  $\mu$  measurements).

Why does neutron in  $^{176}\text{Au}$  occupy  $f_{7/2}$  instead of expected  $h_{9/2}$  orbital?

# Nuclear shells below N = 100

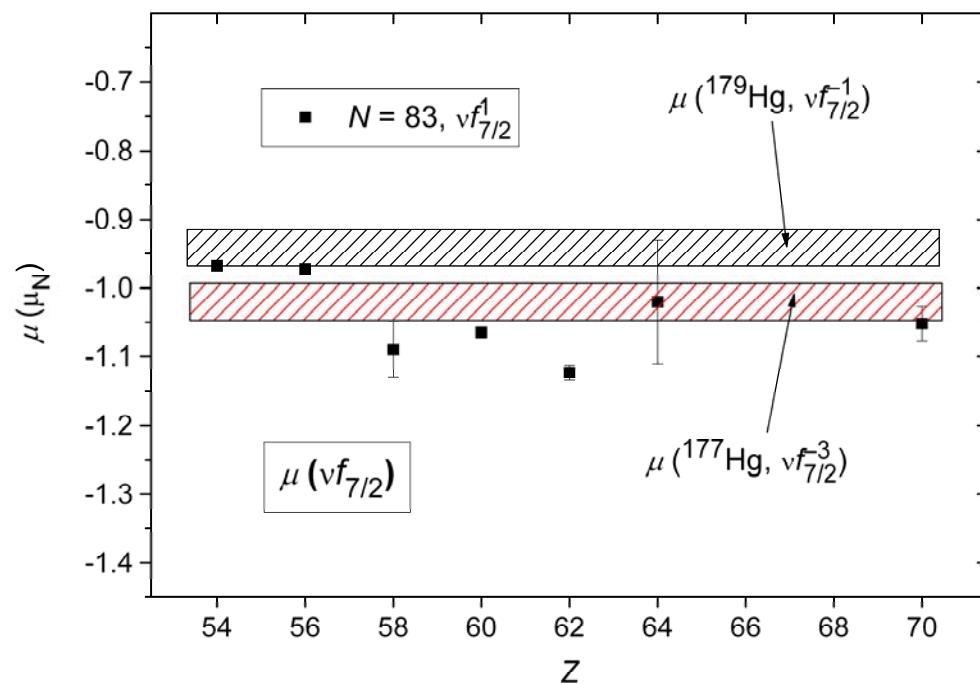
Near stability



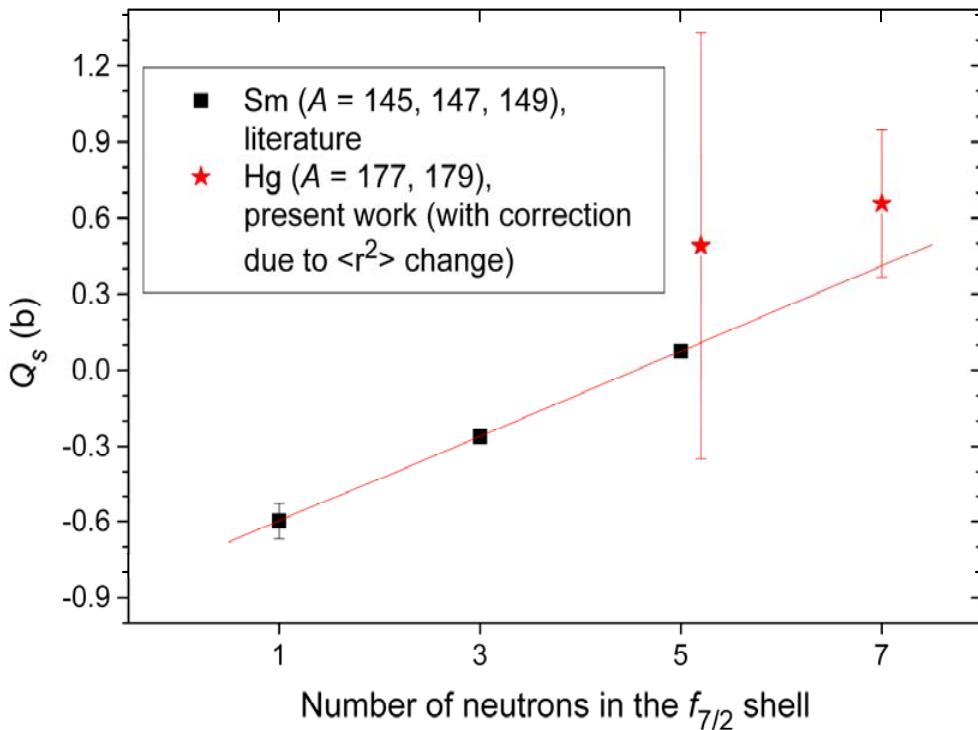
All N = 83 (85) nuclei are of  $vf_{7/2}$  configuration:  
spin, parity,  $\mu$  (from  $^{54}\text{Xe}_{83}$  to  $^{70}\text{Yb}_{83}$ )

N = 99:  $^{181}\text{Pb}_{99}$ , 9/2 $-$ ,  $vh_{9/2}$

$^{179,177}\text{Hg}_{99,97}$ , 7/2 $-$  and  $\mu$  coincides with  $\mu(N = 83)$



# Nuclear shells below N = 100

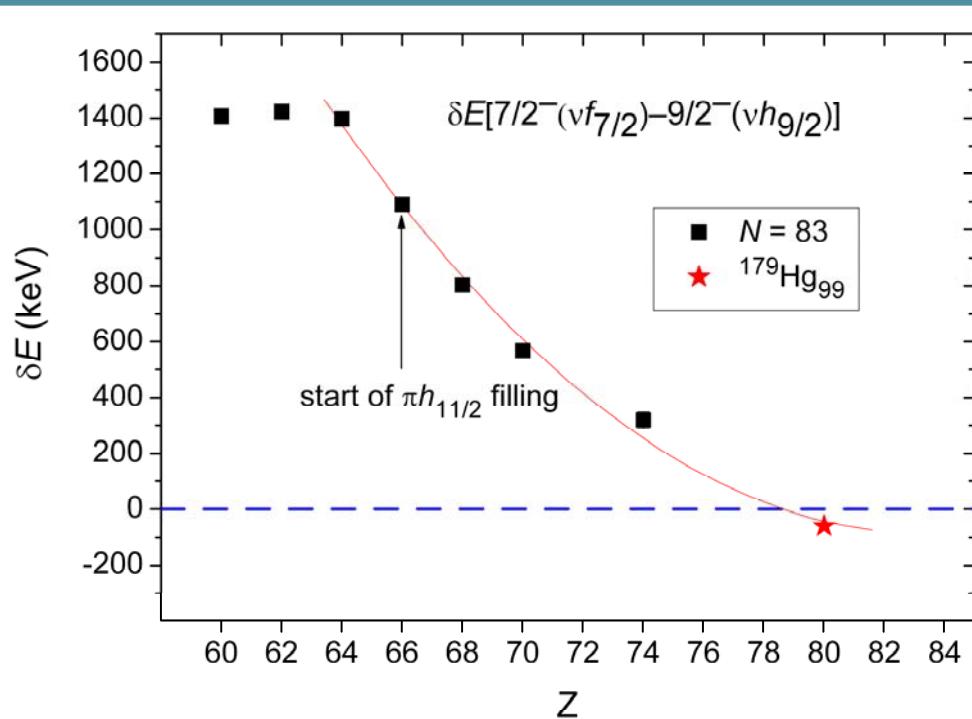


Pure shell model — seniority scheme for the filling  $j$ -shell ( $n$  is a number of neutrons): linear dependence of  $Q_s$  on  $n$

Exp. data for  $Q$  confirm the pure shell-model  $f_{7/2}$  configuration for  $^{177,179}\text{Hg}_{97,99}$

$$\left\langle j^n | \hat{Q} | j^n \right\rangle = \frac{2j+1-2n}{2j+1-2\nu} \left\langle j' | \hat{Q} | j' \right\rangle = \frac{5}{3} Q_{s.p.}(\nu f_{7/2}) - \frac{1}{3} Q_{s.p.}(\nu f_{7/2}) \cdot n$$

# Shell evolution



$^{160}\text{Re}_{85}$ : Changing single-particle structure beyond the proton drip line

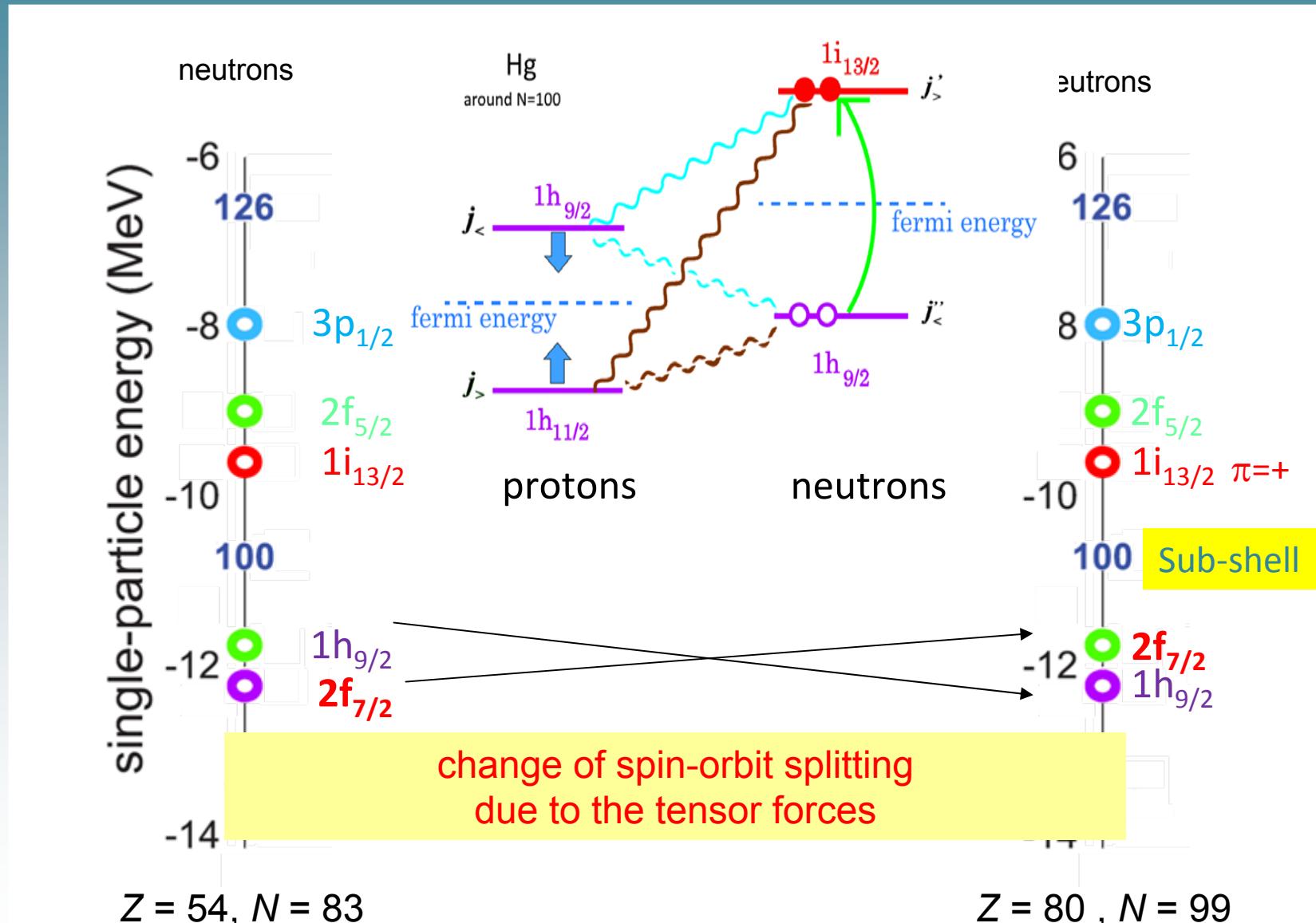
The convergence of the  $h_{9/2}$  and  $f_{7/2}$  neutron levels could open up a  $\gamma$ -decay path from the high-spin isomer to the low-spin ground state of  $^{160}\text{Re}$ , providing a natural explanation for the anomalous absence of charged-particle emission.

I.G. Darby et al. Phys. Lett. B 695 (2011) 78

One expects the proton–neutron tensor force component acting between protons filling the  $1h_{11/2}$  orbital and a single neutron in the  $1h_{9/2}$  or  $2f_{7/2}$  orbitals to modify their relative single-particle energies

L. Bianco et al. / Physics Letters B 690 (2010) 15

# Shell swap



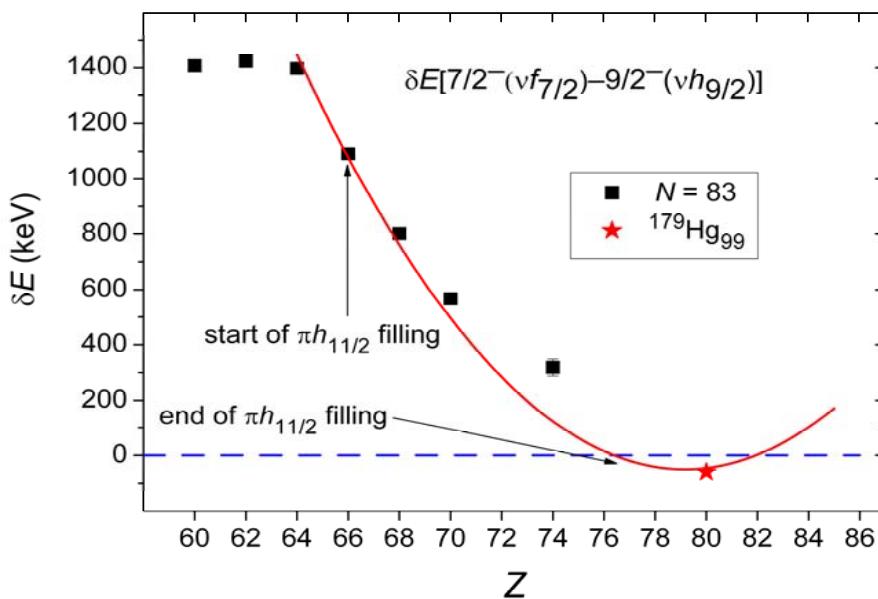
# Shell swap

Au

Configuration	$I$	$\mu_{\text{add}}(\mu_N)$	$\mu_{\text{exp}}(\mu_N)$
$\pi d_{3/2} \otimes vh_{9/2}$	4	-0.84	-0.834(9)
$\pi d_{3/2} \otimes h_{9/2}$	4	0.66	-0.834(9)

Tl

Configuration	$I$	$\mu_{\text{add}}(\mu_N)$	$\mu_{\text{exp}}(\mu_N)$
$\pi s_{1/2} \otimes vh_{9/2}$	4	-0.58	-0.564(23)
$\pi s_{1/2} \otimes vf_{7/2}$	4	0.70	-0.564(23)



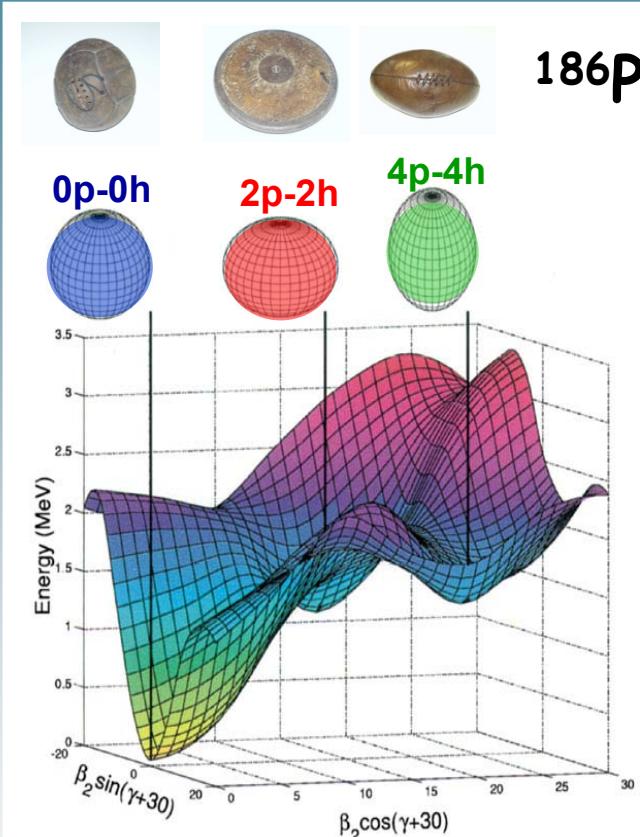
$\mu(^{176}\text{Au}_{97})$  is explained only with  $vf_{7/2}$  assumption for neutron configuration (additivity relation)

$\mu(^{180}\text{Tl}_{99})$  is explained only with  $vh_{9/2}$  assumption for neutron configuration

$^{181}\text{Pb}_{99} - vh_{9/2}$  configuration:  
 $I(^{181}\text{Pb}_{99}) = 9/2$

Subshells return to the “normal” ordering at  $Z > 80$

# Shape Coexistence in the Pb region

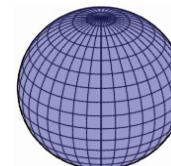


Potential Energy Surface for  $^{186}\text{Pb}$

A. Andreyev et al. Nature, 405, 430 (2000)

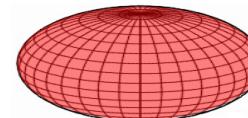
$^{186}\text{Pb}$

- Pb ( $Z=82$ ) g.s.: p(0p-0h) – spherical

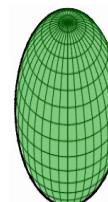


**Proton pair excitations** across  $Z=82$  shell gap (neutrons are spectators):

- 1 pair excitation: p(2p-2h) -oblate



- 2 pair excitation: p(4p-4h) -prolate



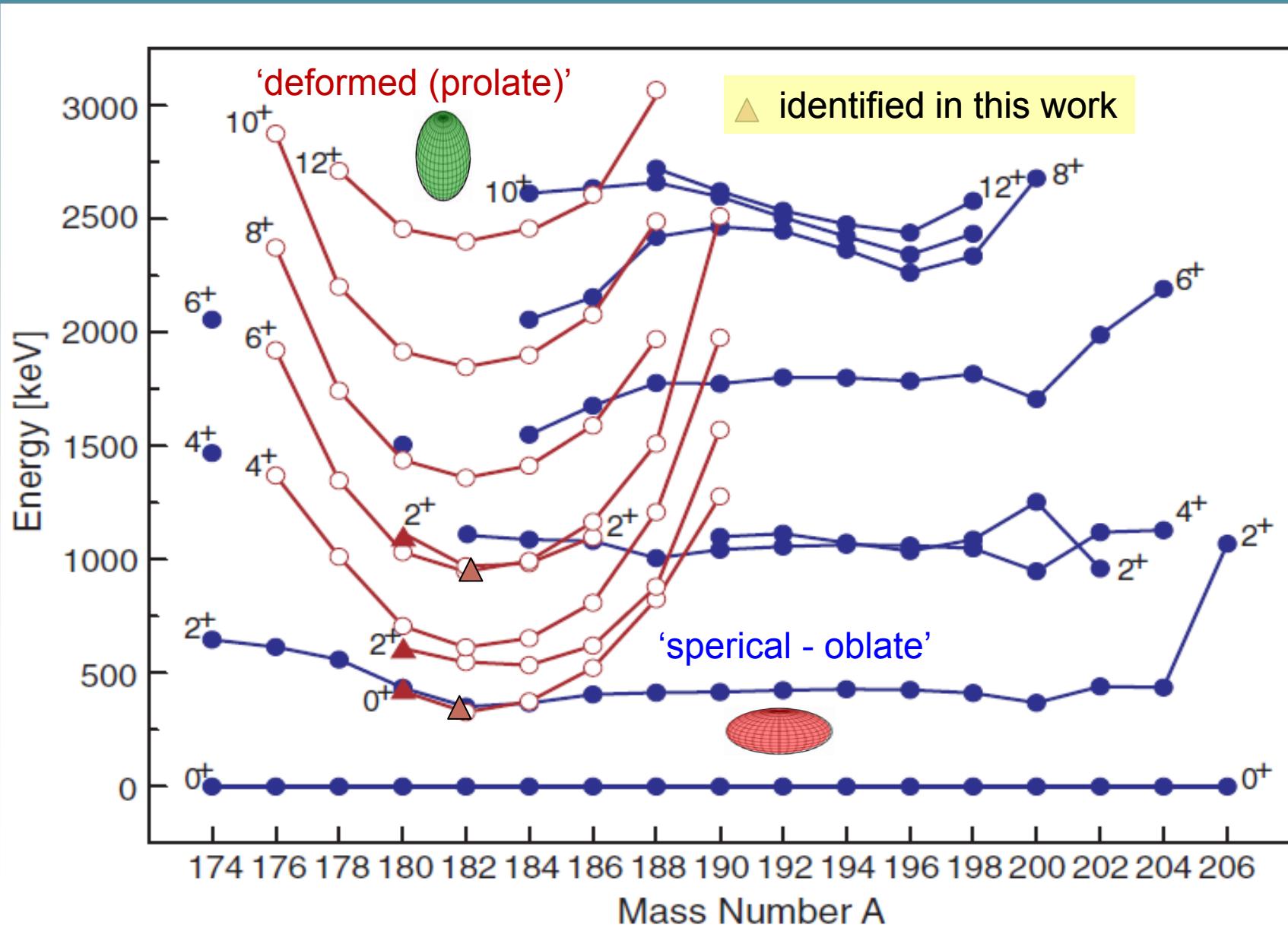
K. Heyde et al., Phys. Rep. 102 (1983) 291

J.L. Wood et al., Phys. Rep. 215 (1992) 101

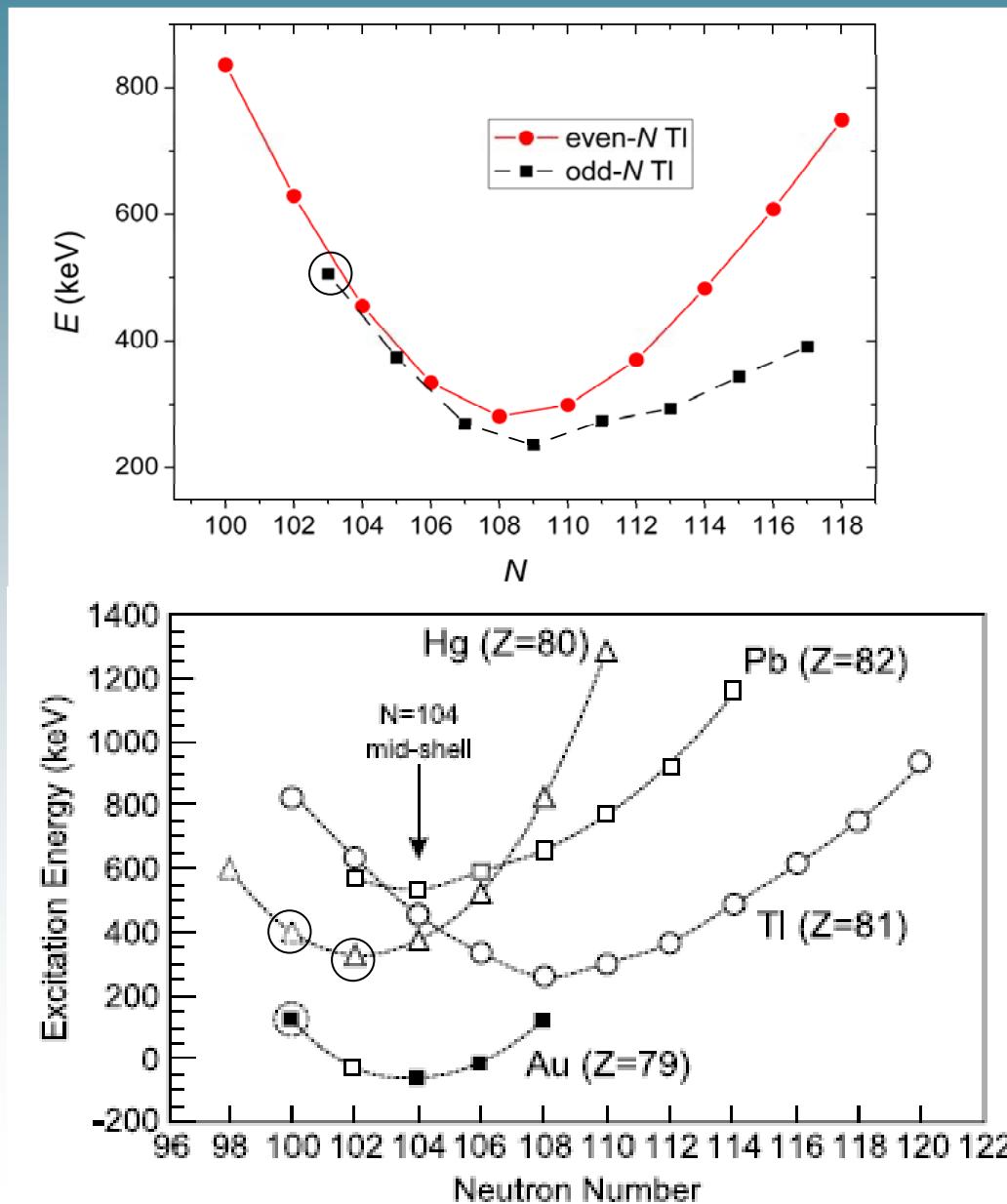
A. Andreyev et al., Nature 405 (2000) 430

**K. Heyde and J. Wood, Rev. Mod. Phys., 83, 1467 (2011)**

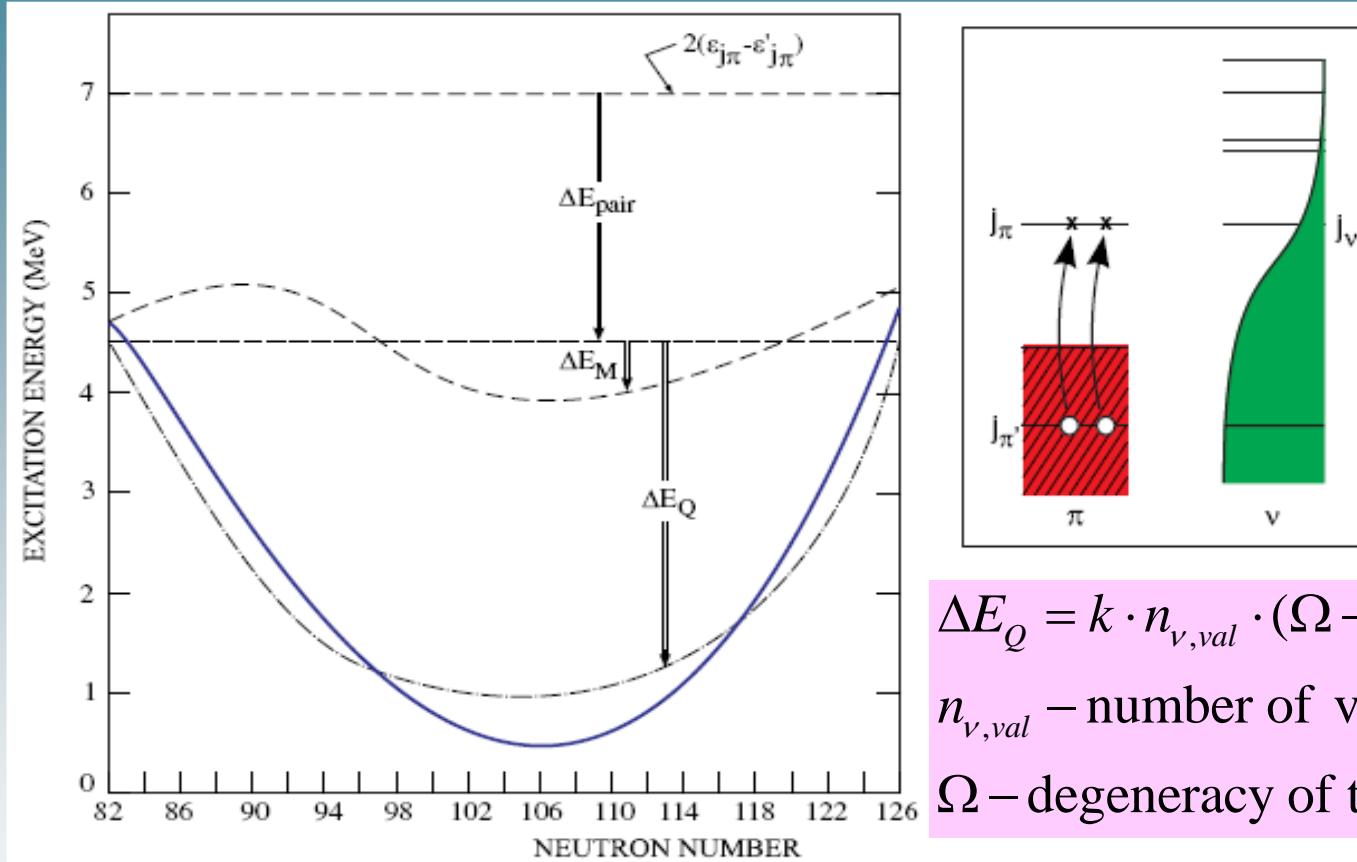
# Mercury Chain (Z=80)



# Intruder states



# Intruder states



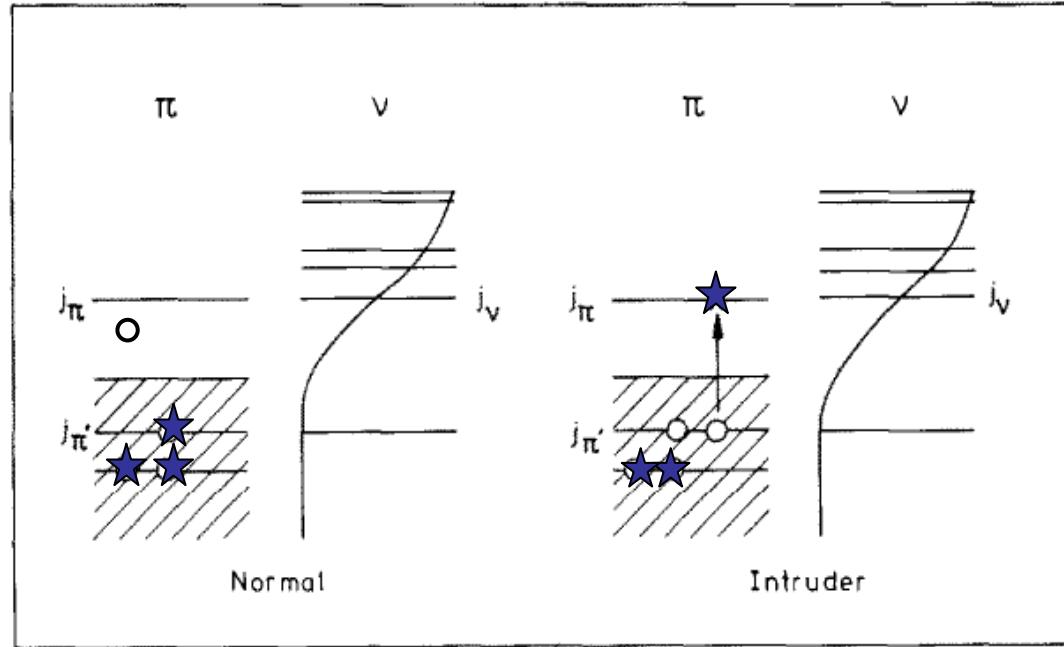
$$\Delta E_Q = k \cdot n_{\nu, val} \cdot (\Omega - n_{\nu, val}) \cdot n_{p-h}$$

$n_{\nu, val}$  – number of valence neutrons

$\Omega$  – degeneracy of the neutron shell

The different energy terms, contributing to the energy of the lowest proton 2p-2h 0<sup>+</sup> intruder state for heavy nuclei. The unperturbed energy, the pairing energy, the monopole energy shift, and the quadrupole energy gain are presented,

# Intruder states



Schematic representation of a proton 1p2h intruder configuration (TI)

# Mixing of configurations with different shapes

$\alpha_C(2_2^+ \rightarrow 2_1^+)$ :

$^{180}\text{Hg}$	3.5(4)	E0 transition exists
$^{182}\text{Hg}$	7.2(13) [cf. $\alpha_C(\text{M1}) = 1.15$ ; $\alpha_C(\text{E2}) = 0.42$ ]	
$^{184}\text{Hg}$	14.2(3.6)	

$$\rho^2(E0) = \frac{Z^2}{R_0^2} a^2 (1 - a^2) [\delta \langle r^2 \rangle]^2$$

The large conversion coefficient for the  $2_2^+$  to  $2_1^+$  transition in  $^{182,184}\text{Hg}$  is a strong fingerprint of shape coexistence as strong E0 transitions are the result of considerable mixing of two states with a large difference in deformation. Combining the measured conversion coefficients with the re-evaluated  $B(\text{E2})$  values from the Coulomb excitation experiments will result in E0 transition strength  $\rho^2(\text{E0})$  values which can be compared with different theoretical models

# Conclusions

Изомерно селективная фотоионизация в лазерном ионном источнике позволяет получить большой объем ядерно-спектроскопической информации ( $T_{1/2}$ ,  $E_\alpha$ ,  $b_\alpha$ ,  $b_\beta$ ,  $\alpha\text{-}\gamma$ ,  $\gamma\text{-}\gamma$  coincidence, conversion coefficients, partial decay schemes и т. д.) без дополнительных затрат времени.

Из полученных результатов отметим:

1. Сопоставление фактора задержки  $\alpha$  распада  $^{181}\text{TI} \rightarrow ^{177}\text{Au}$  со спинами и магнитными моментами этих ядер позволяет сделать вывод о неаксиальной деформации  $^{177}\text{Au}$ ;
2. Большой фактор задержки  $\alpha$  распада  $^{180}\text{TI} \rightarrow ^{176}\text{Au}$ , а также анализ спинов и моментов соседних изотопов Hg указывает на изменение оболочечной структуры (shell swap).
3. Обнаружен новый интрудер изомер в  $^{184}\text{TI}$ , подтверждена параболическая зависимость энергии возбуждения этих изомеров от числа нейтронов.
4. Аномально большие коэффициенты конверсии для  $2_2^+ \rightarrow 2_1^+$  переходов в  $^{180,182,184}\text{Hg}$  свидетельствуют о сильном смешивании состояний с разной деформацией.