

ПРЕЦИЗИОННОЕ ИЗМЕРЕНИЕ СКОРОСТИ ЗАХВАТА МЮОНА В ВОДОРОДЕ И ОПРЕДЕЛЕНИЕ ПСЕВДОСКАЛЯРНОГО ФОРМ ФАКТОРА ПРОТОНА g_p

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Precision Measurement of Muon Capture on the Proton “ *μ Cap experiment*”



www.npl.uiuc.edu/exp/mucapture/

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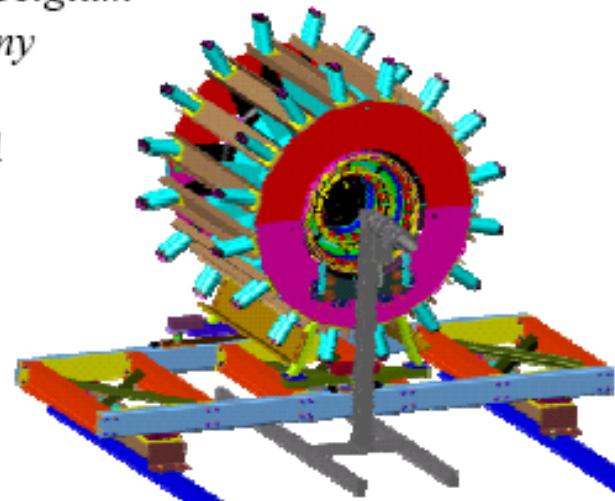
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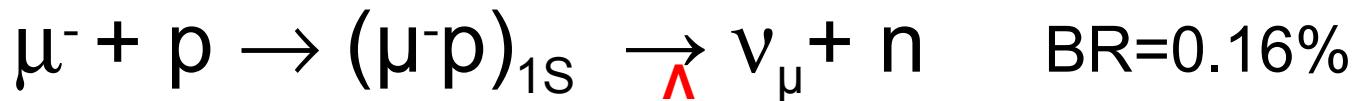
TU Munich, Garching, Germany

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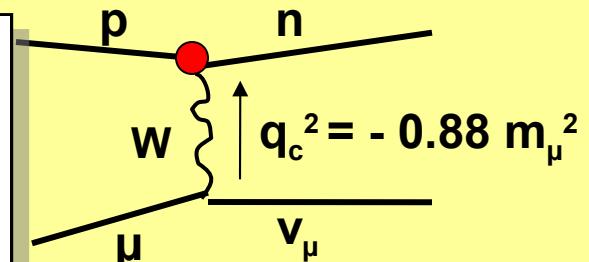


Muon Capture on Proton



MuCap goal: to measure μp -capture rate Λ with 1% (or better) precision

$$V_\alpha = g_V(q^2) \gamma_\alpha + \frac{i g_M(q^2)}{2 M_N} \sigma_{\alpha\beta} q^\beta$$
$$A_\alpha = g_A(q^2) \gamma_\alpha \gamma_5 + \frac{\mathbf{g}_P(q^2)}{m_\mu} q_\alpha \gamma_5$$



μp-capture offers a unique probe of the nucleon's electroweak axial structure

Muon capture on proton

$$V_\alpha = g_V(q^2) \gamma_\alpha + \frac{i g_M(q^2)}{2 M_N} \sigma_{\alpha\beta} q^\beta$$

$$A_\alpha = g_A(q^2) \gamma_\alpha \gamma_5 + \frac{\textcolor{red}{g}_P(q^2)}{m_\mu} q_\alpha \gamma_5$$

Стандартная Модель и структура нуклонов

$$g_v = 0.9755 \pm 0.0005$$

$$g_a = 1.245 \pm 0.003$$

$$g_m = 3.582 \pm 0.003$$

$$g_P(\text{th}) = 8.26 \pm 0.23$$

$$g_P(\text{OMC}) = 6 - 12$$

$$g_P(\text{RMC}) = 12.2 \pm 0.9 \pm 0.4$$

pseudoscalar form factor g_P

PCAC:

$$g_P(q^2) = \frac{2m_\mu M}{m_\pi^2 - q^2} g_A(0)$$

$$g_P = 8.7$$

heavy baryon chiral perturbation theory:

$$g_P(q^2) = \frac{2m_\mu g_{\pi NN} F_\pi}{m_\pi^2 - q^2} - \frac{1}{3} g_A(0) m_\mu M r_A^2$$

$$g_P = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.23$$

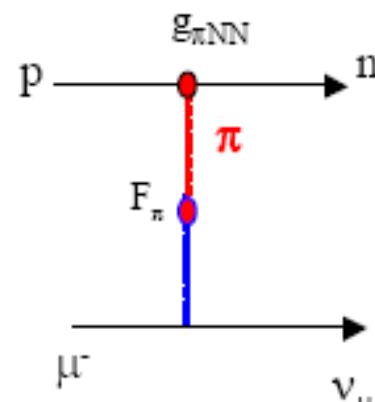
Λ calculations $O(p^3)$ show good convergence: 100 %
 delta effect small LO 25 % NLO 3 %
 LO NLO NNLO

| |
|--------------|
| $g_{\pi NN}$ |
| 13.31(34) |
| 13.0(1) |
| 13.05(8) |

| author | year | g_P | Λ_S | Λ_T | comment |
|----------------|--------|-----------|--------------|-------------|-------------------|
| Primakoff | 1959 | | 664(20) | 11.9(7) | smaller g_A |
| Opat | 1964 | | 634 | 13.3 | smaller g_A |
| Bernard et al | 1994 | 8.44(23) | | | |
| Fearing et al | 1997 | 8.21(9) | | | |
| Govaerts et al | 2000 | 8.475(76) | 688.4(38) | 12.01(12) | |
| Bernard et al | 2000/1 | | 687.4 (711*) | 12.9 | NNLO, small scale |
| Ando et al | 2001 | | 695 (722*) | 11.9 | NNLO |

*NLO result

μ Cap

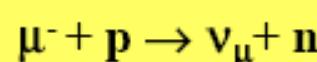


Muon capture on proton Sensitivity to Form Factors

$$\frac{\delta \Lambda_S}{\Lambda_S} = 2 \frac{\delta V_{ud}}{V_{ud}} + 0.466 \frac{\delta g_v}{g_v} + 0.151 \frac{\delta g_m}{g_m} + 1.567 \frac{\delta g_a}{g_a} - 0.179 \frac{\delta g_p}{g_p}$$

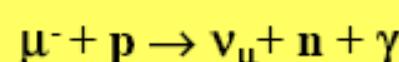
Experimental information on g_p

Ordinary Muon Capture



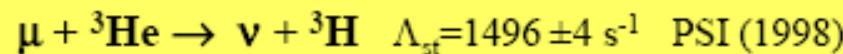
BR~ 10^{-3} , 8 experiments 1962-82, BC, neutron, electron detection
“in principle” most direct g_p measurement

Radiative Muon Capture



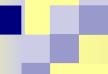
BR~ 10^{-8} , TRIUMF (1998), $E_\gamma > 60$ MeV, 297 ± 26 events
closer to pion pole → *3x sensitivity of OMC*
theory more involved (min substitution, ChPT)

- Muon capture in nuclei



$g_p = g_p^{\text{th}} (1.08 \pm 0.19)$ error dominated by 3-N theory
correlation measurements

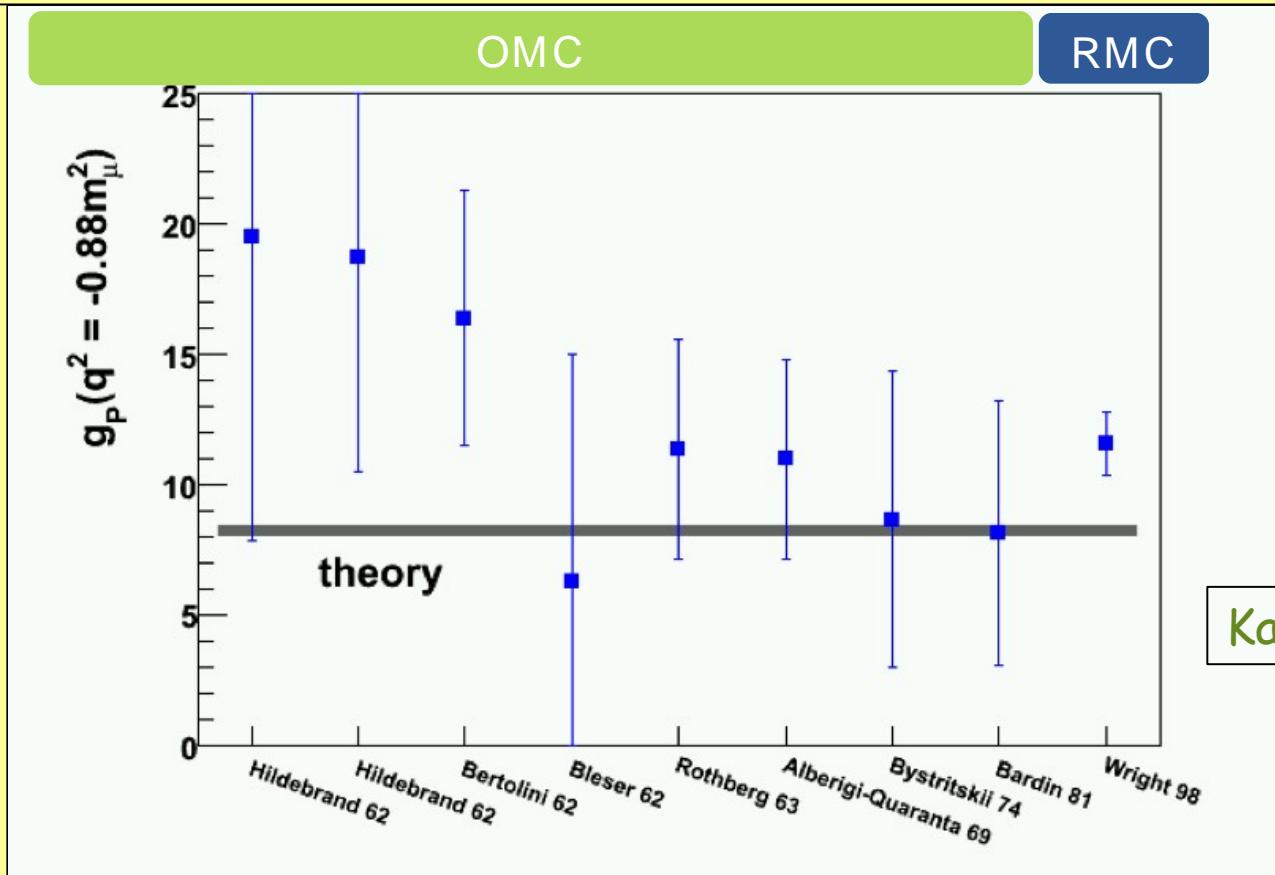
- π electro production at threshold



| Ref. | n/n_o | Δt (μs) | S:O:P | Rate (s^{-1}) | $g_p(-0.88m_\mu^2)$ |
|---|-----------------|------------------------|----------------|----------------------------------|------------------------|
| Ordinary muon capture | | | | | |
| Hildebrand (1962) | 1.0 | 0.0 | 0.15:0.77:0.07 | 420 ± 120 | 19.5 ± 11.6 |
| Hildebrand and Doede (1962) | 1.0 | 0.0 | 0.15:0.77:0.07 | 428 ± 85 | 18.7 ± 8.2 |
| Bertolini <i>et al.</i> (1962) | 1.0 | 0.0 | 0.15:0.77:0.07 | 450 ± 50 | 16.4 ± 4.9 |
| Bleser <i>et al.</i> (1962) | 1.0 | 1.0 | 0.01:0.88:0.11 | 515 ± 85 | 6.3 ± 8.7 |
| Rothberg <i>et al.</i> (1963) | 1.0 | 1.2 | 0.01:0.88:0.12 | 464 ± 42 | 11.4 ± 4.2 |
| Alberigi-Quaranta <i>et al.</i> (1969) | 0.014 | 0.9 | 1.00:0.00:0.00 | 651 ± 57 | 11.0 ± 3.8 |
| Bystritskii <i>et al.</i> (1974) | 0.072 | 1.4 | 1.00:0.00:0.00 | 686 ± 88 | 8.7 ± 5.7 |
| Bardin <i>et al.</i> (1981a) (original τ_+) | 1.0 | 2.5 | | 460 ± 20 | 7.9 ± 3.0 |
| | (new τ_+) | | | 435 ± 17 | 10.6 ± 2.7 |
| Radiative muon capture | | | | | |
| Wright <i>et al.</i> (1998) (original theory) | 1.0 | 0.365 | 0.06:0.85:0.09 | $(2.10 \pm 0.21) \times 10^{-8}$ | $12.4 \pm 0.9 \pm 0.4$ |
| | (new theory) | | | | $12.2 \pm 0.9 \pm 0.4$ |

50 years of effort to determine gP

$\mu^+ \odot + u \odot d + \bar{d}$



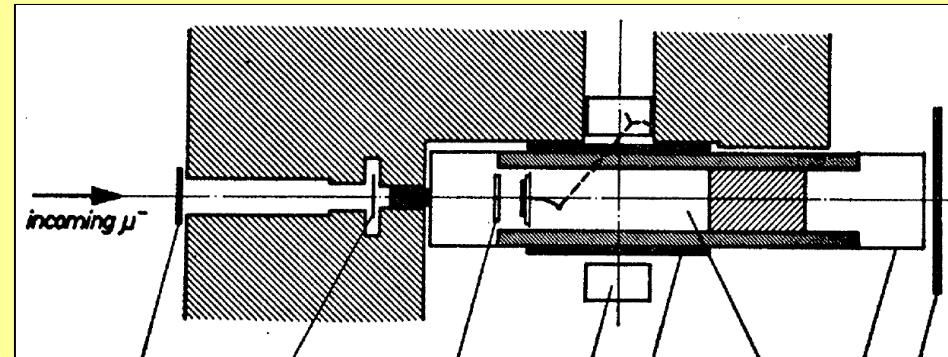
" Radiative muon capture in hydrogen was carried out only recently with the result that the derived g_P was almost 50% too high. If this result is correct, it would be a sign of new physics... "

— Lincoln Wolfenstein (Ann.ReNucl.Part.Sci. 2003)

Pioneers of muon capture experiments



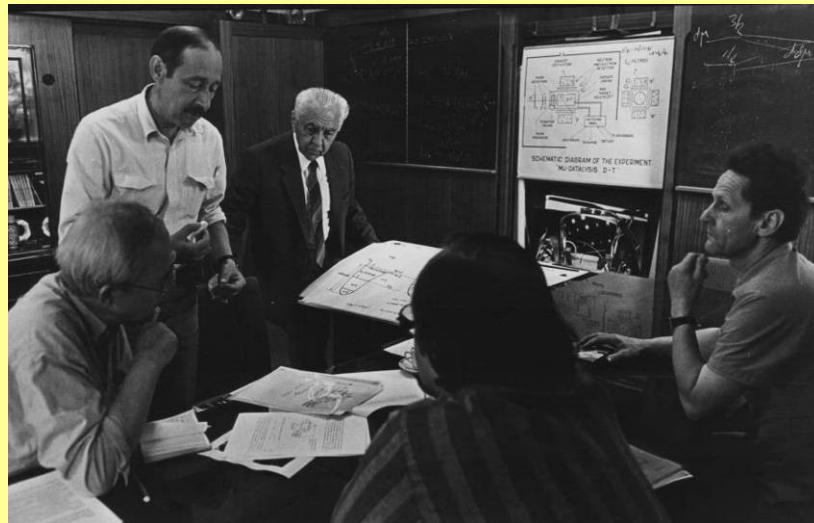
Emilio Zavattini 1927-2007



1969 Bologna-Pisa-CERN

H₂ –target 8 atm

$$g_p = 11.0 \pm 3.8$$



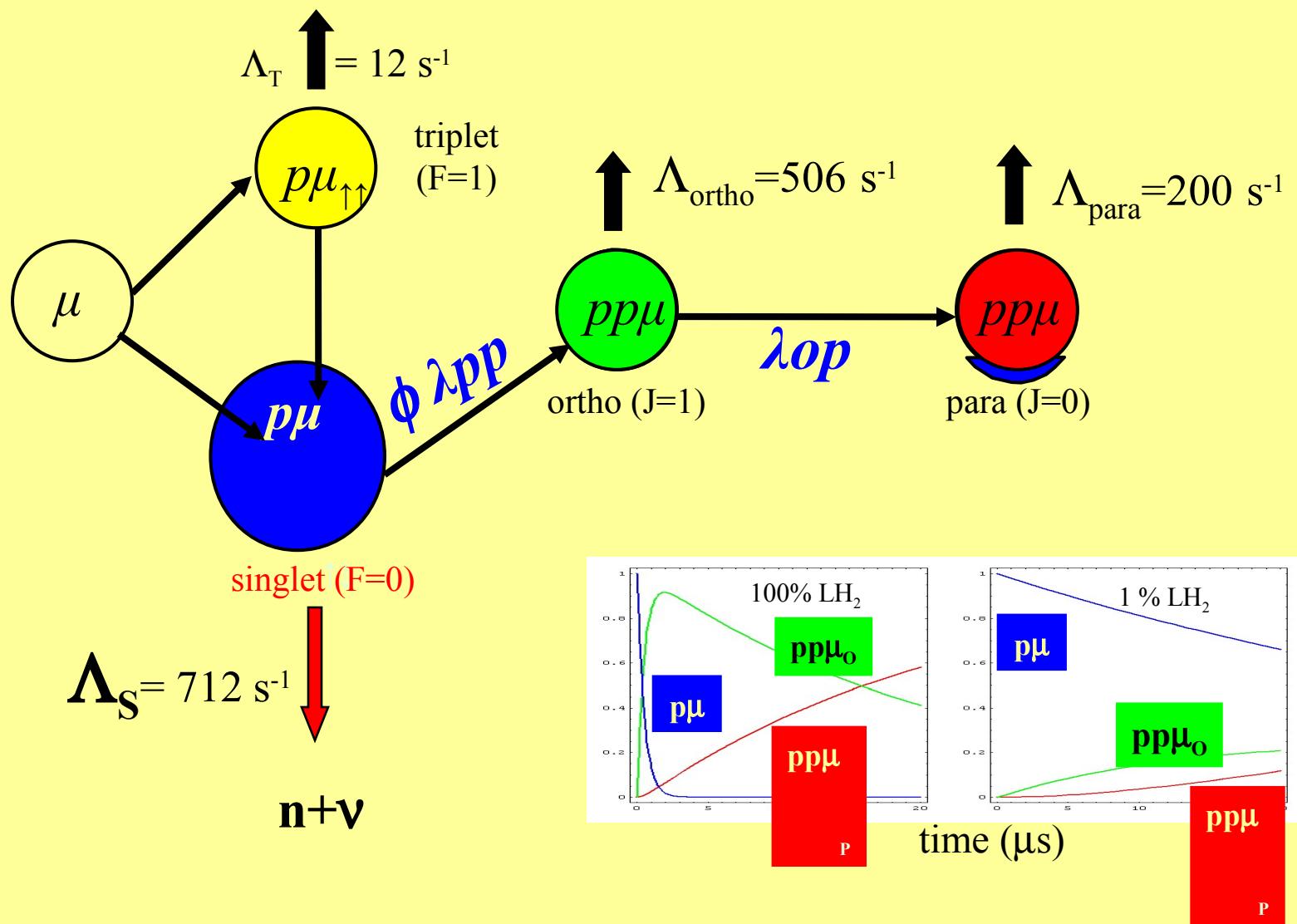
1973 Dubna group

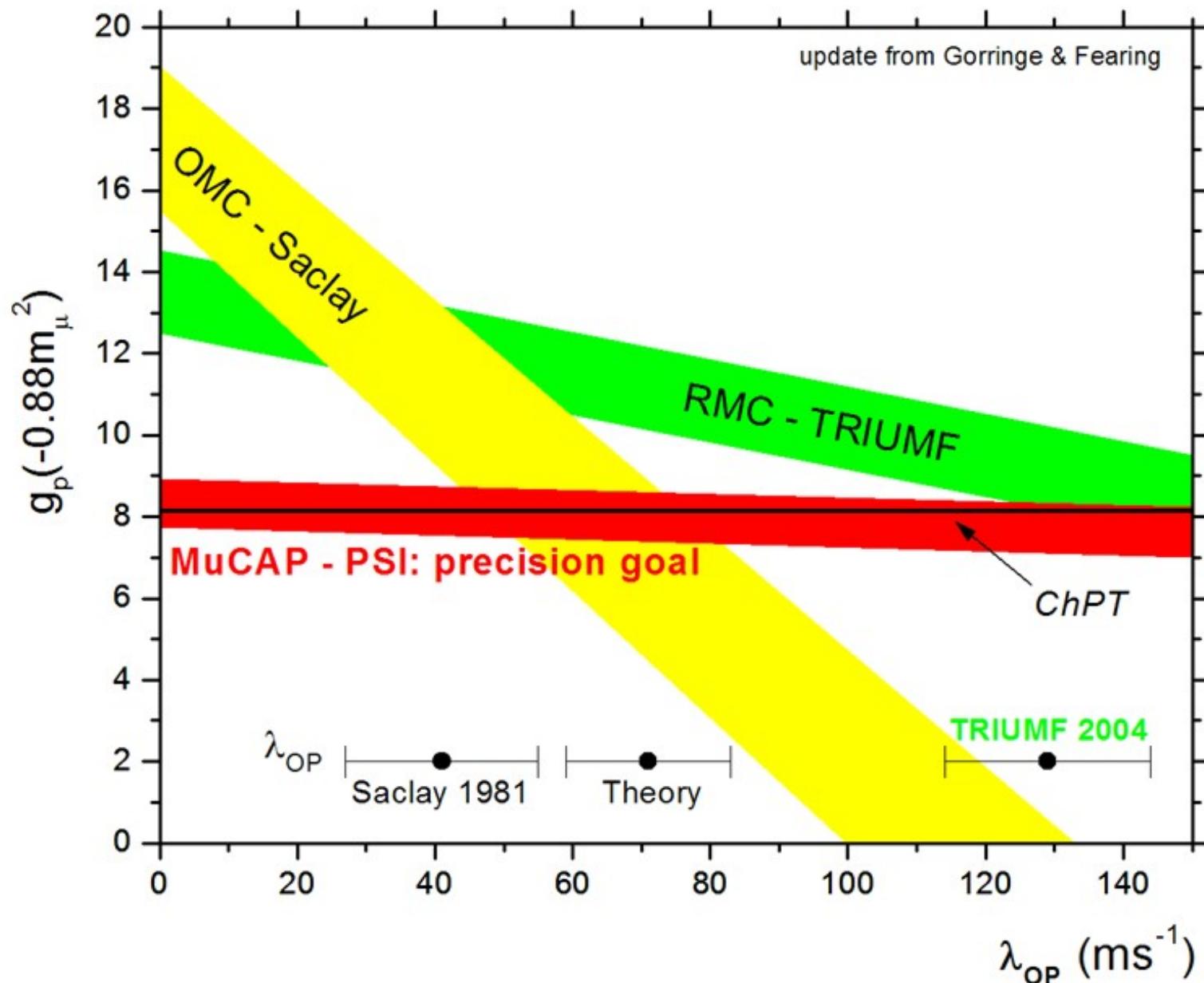
H₂ –target 41 atm

$$g_p = 8.7 \pm 5.7$$

Expt. Problems

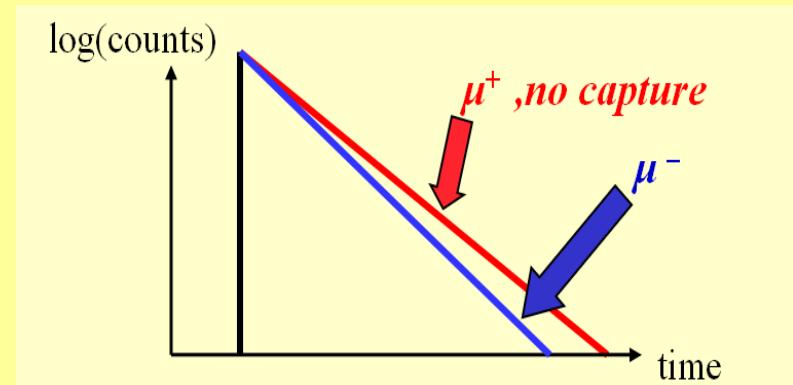
- Wall effects
- Background
- Neutron detection efficiency





Стратегия MuCap эксперимента

- Измерение времени жизни (τ) с точностью 10 ppm, регистрация $\mu \rightarrow eVV$ распадов (10^{10})



- Однозначность интерпретации захвата из $F=0$ состояния μp атома при плотности 1% LH2
- Использование методики активной мишени (TPC)
 - с точной регистрацией координат и времени остановок мюонов, реконструкция треков электронов к точке распада.
- Использование ультрачистого водорода $Cz < 10\text{ppb}$
- Контроль примесей по реакциям: $\mu p + Z \rightarrow \mu Z + p$, $Cz \sim 10\text{ppb}$.
- Обеспечение изотопической чистоты водорода
 $\mu p + d \rightarrow \mu d + p + 134\text{eV}$, примесь Cd < 1 ppm, диффузия $\mu d \sim \text{cm}$

PSI meson factory

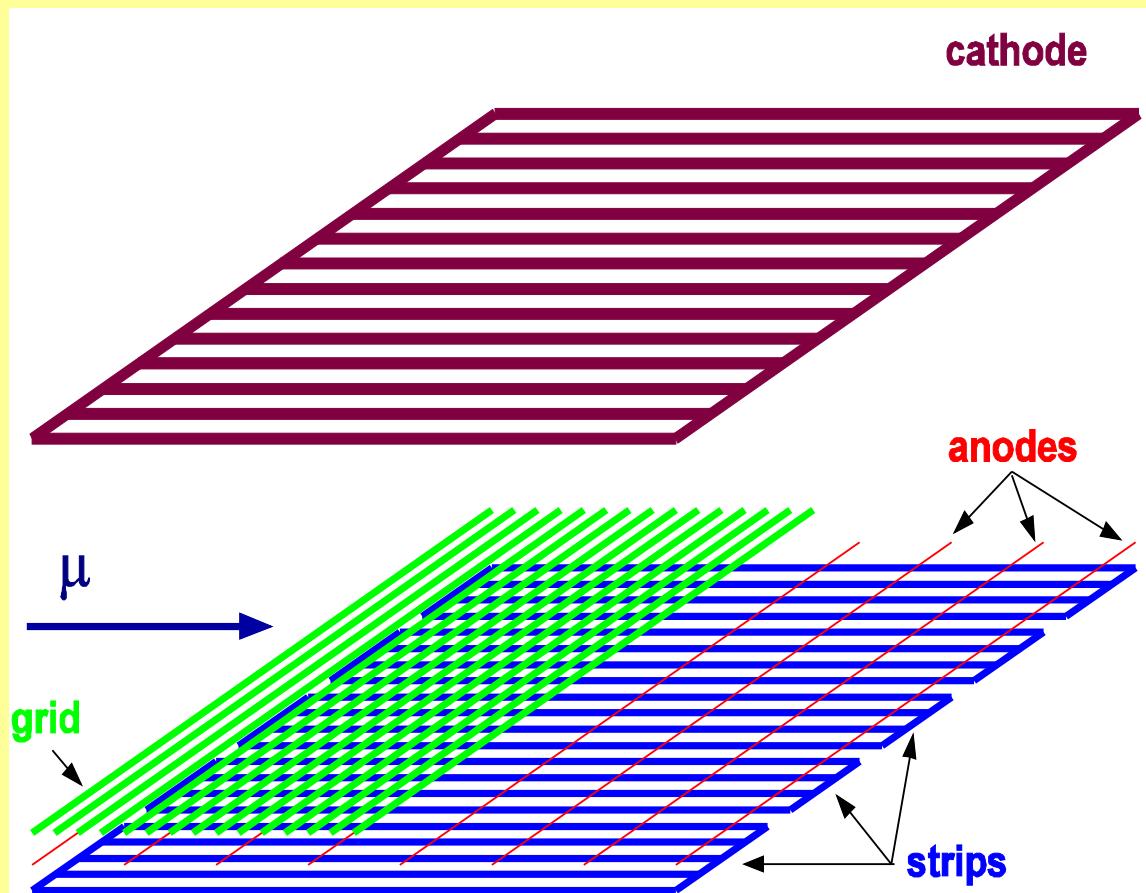


600MeV protons
2mA extracted proton beam
100% duty factor
High intensity muon channels
Muon-on-request mode

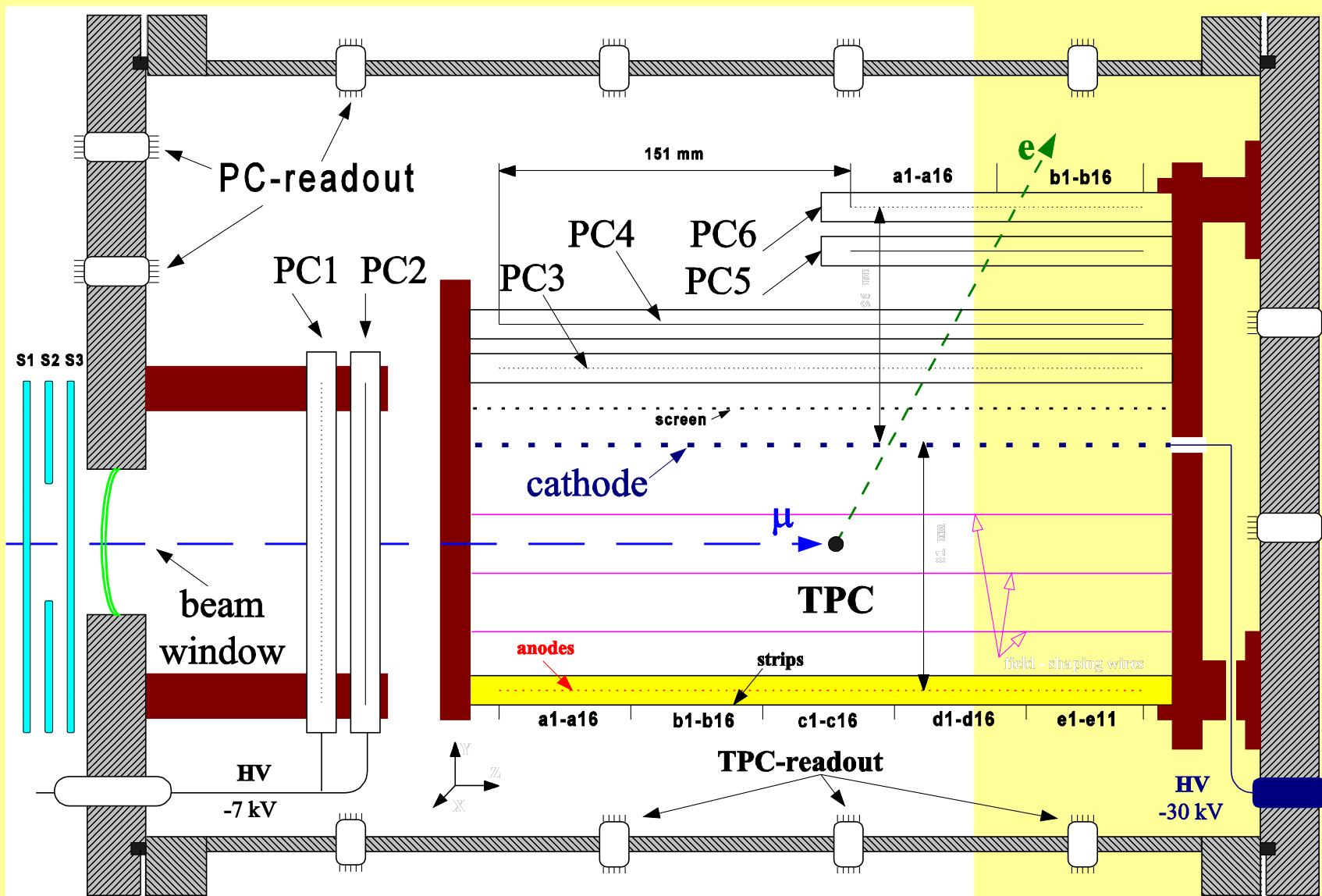
PNPI in PSI since 1986

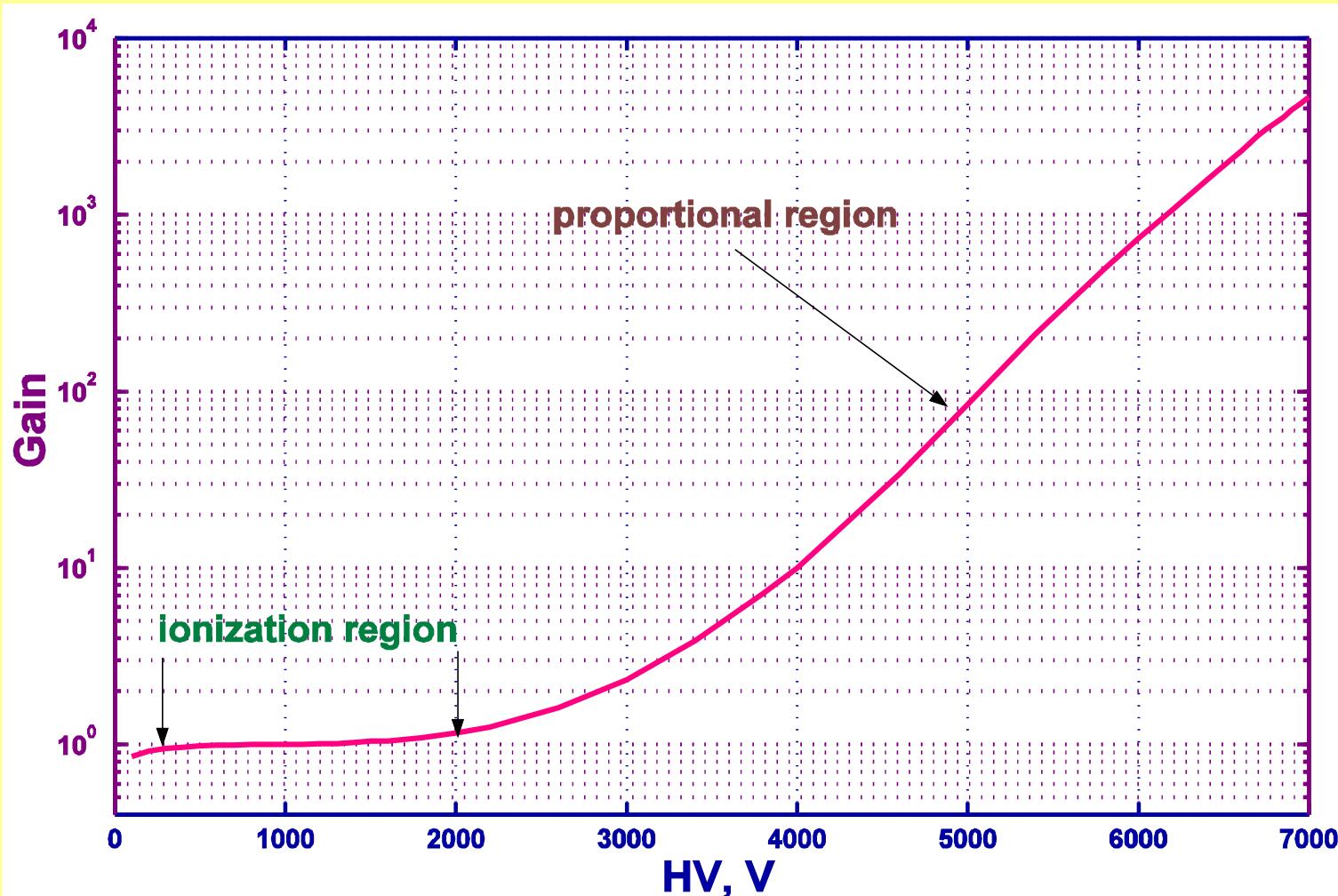
- Muon catalyzed dd-and dt-fusion experiments (completed)
- Muon capture on He-3 (completed)
- Muon capture on proton (completed)
- Muon capture on deuteron (in progress)

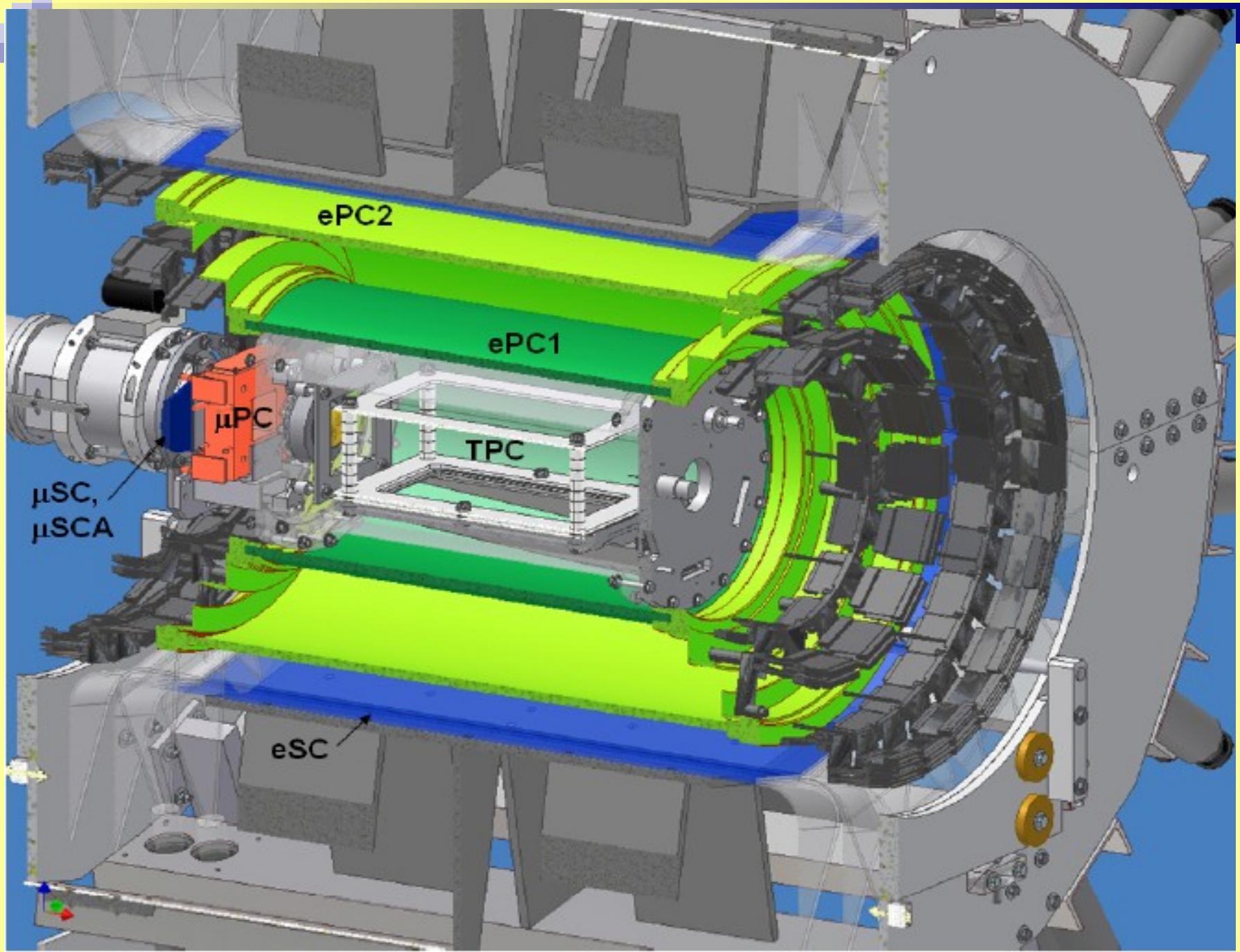
Schematic view of the TPC

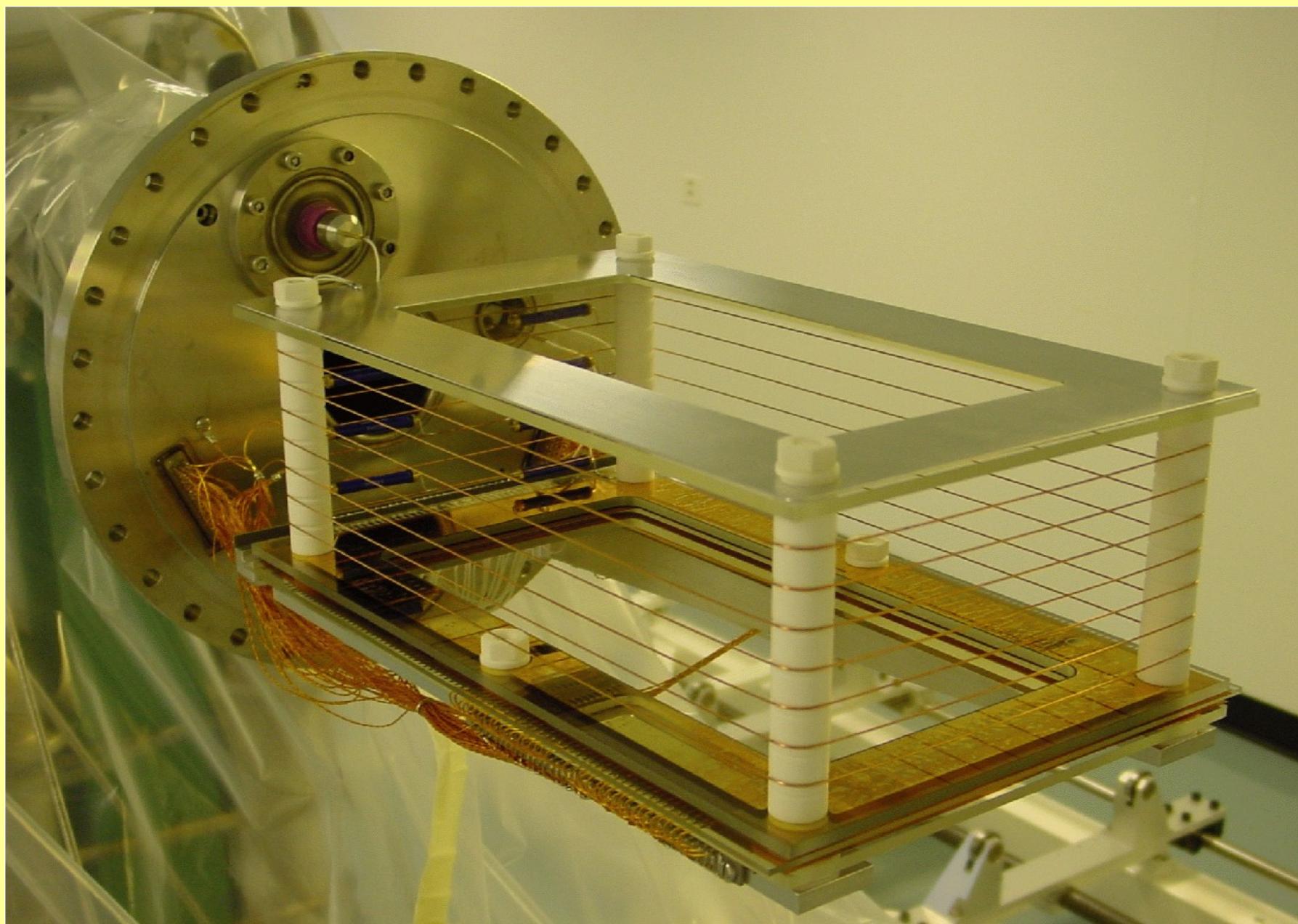


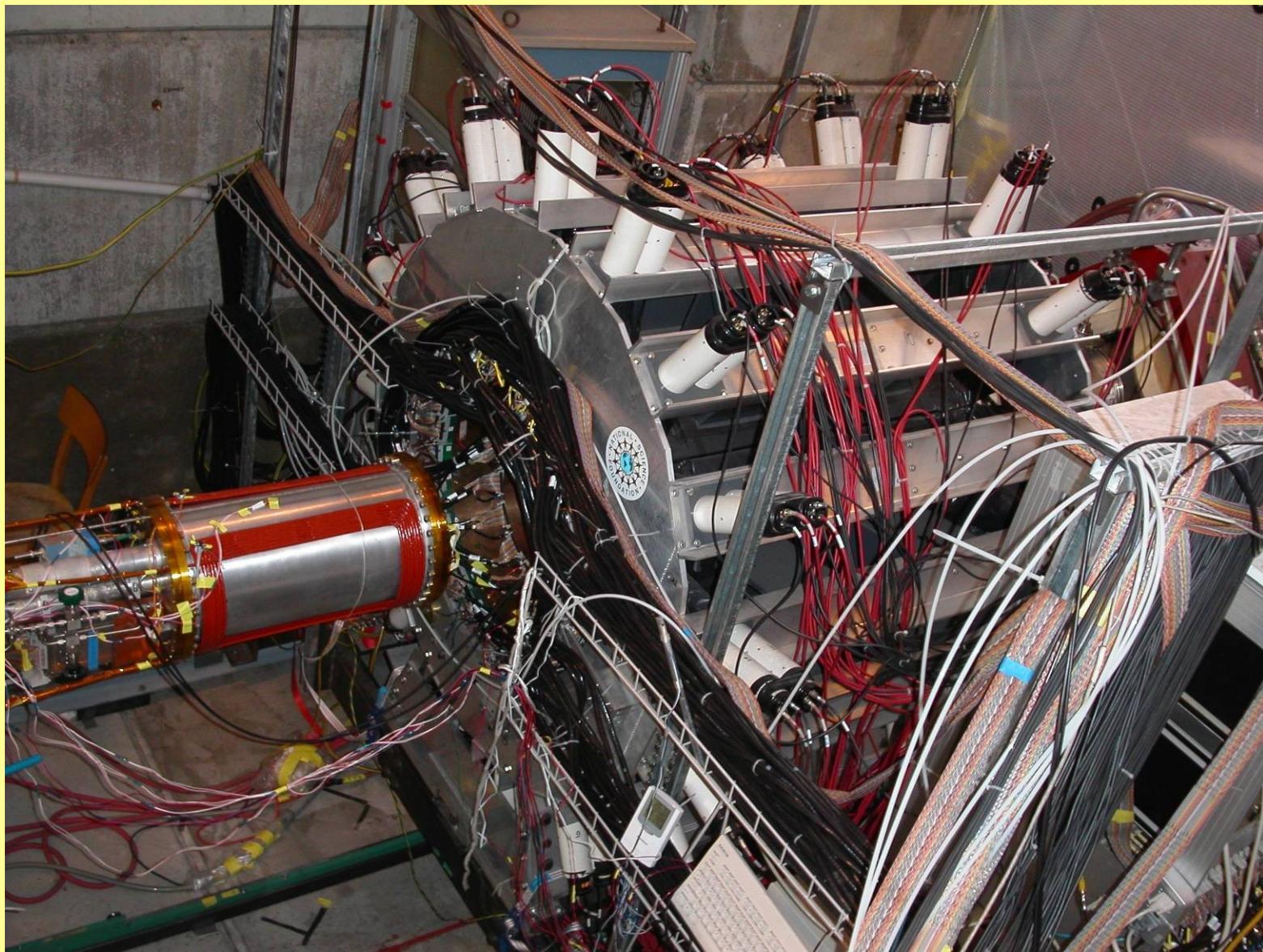
The trajectories of charged particles are measured in 3D space with resolution (rms) 1-2 mm.

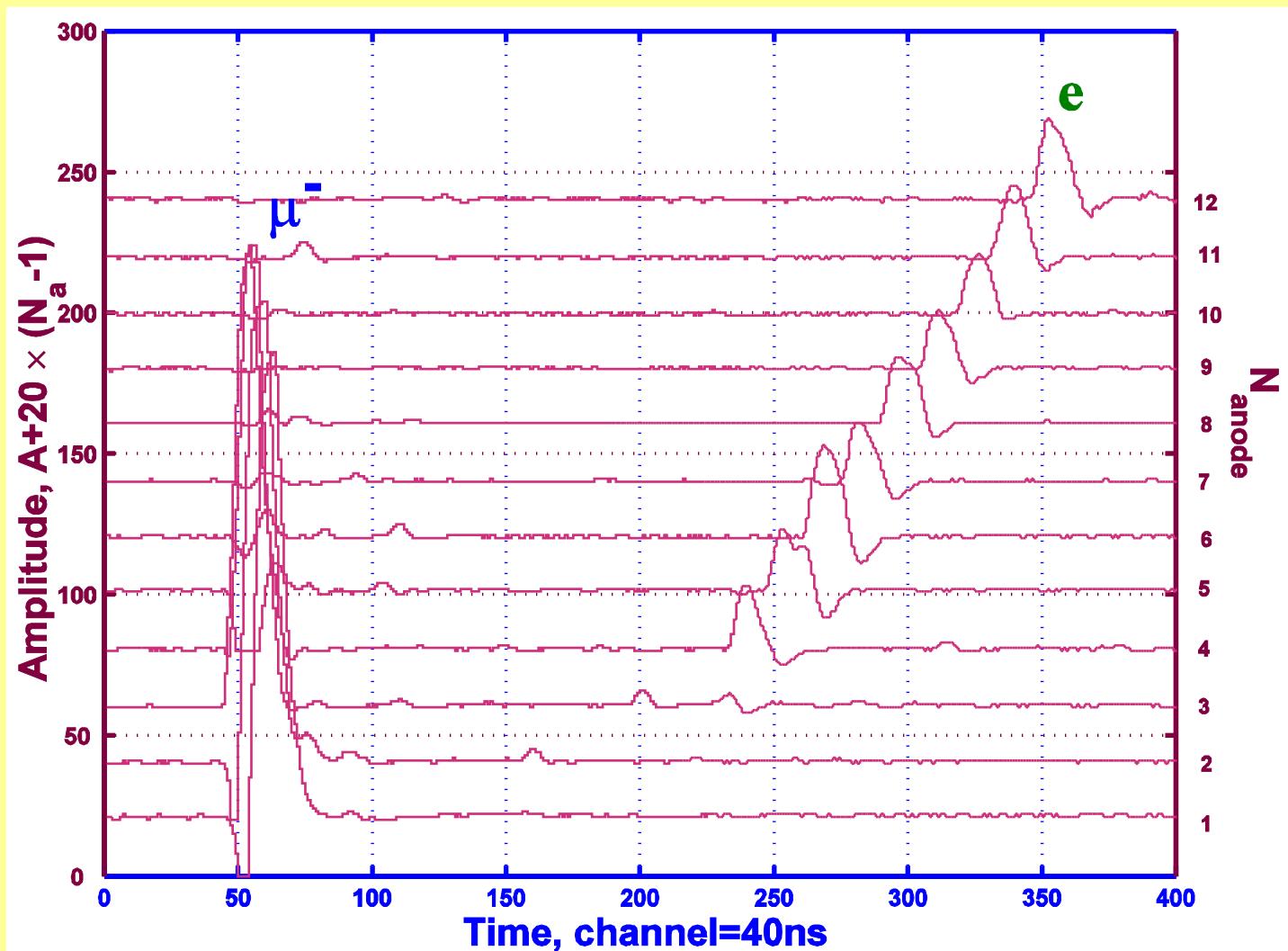






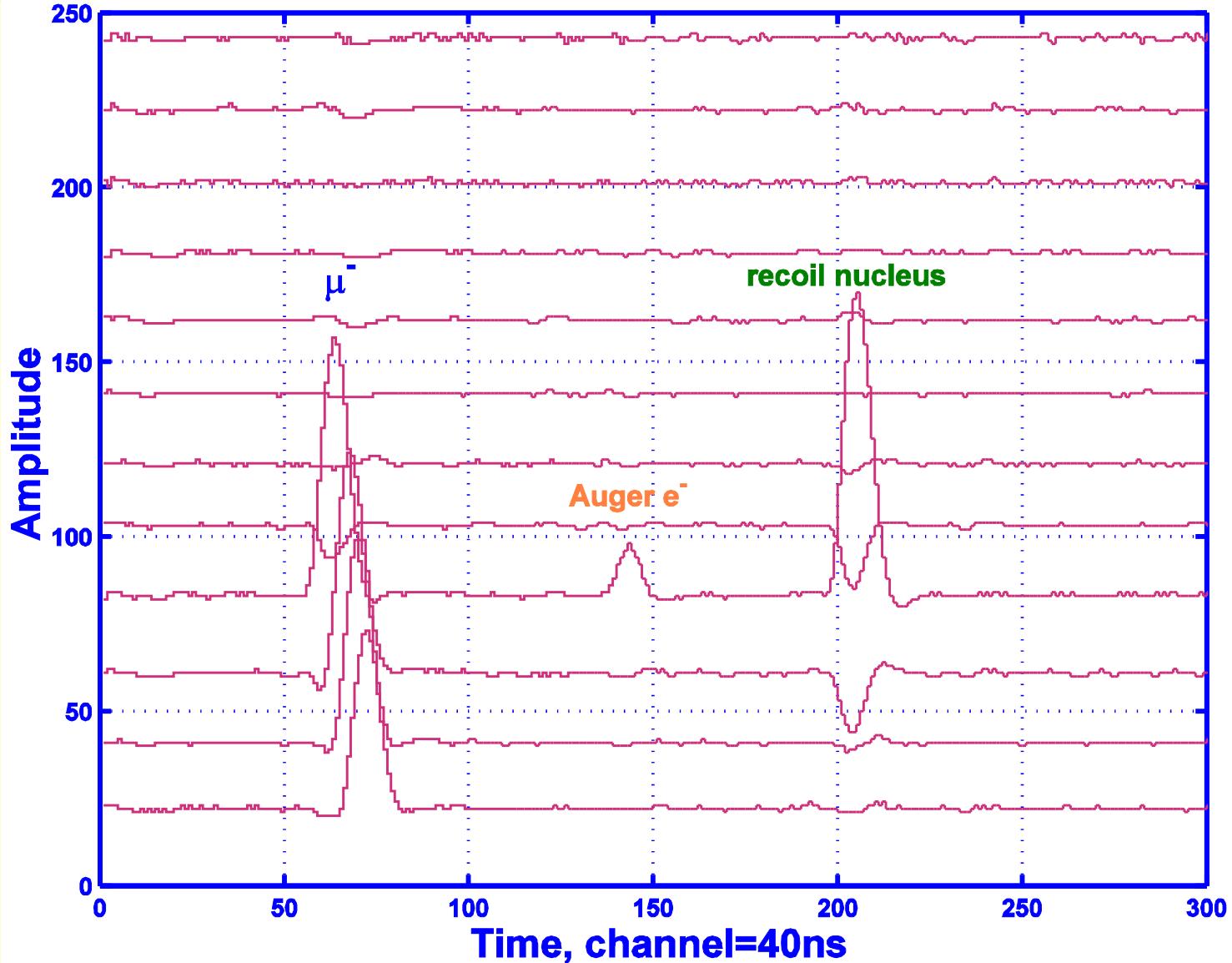




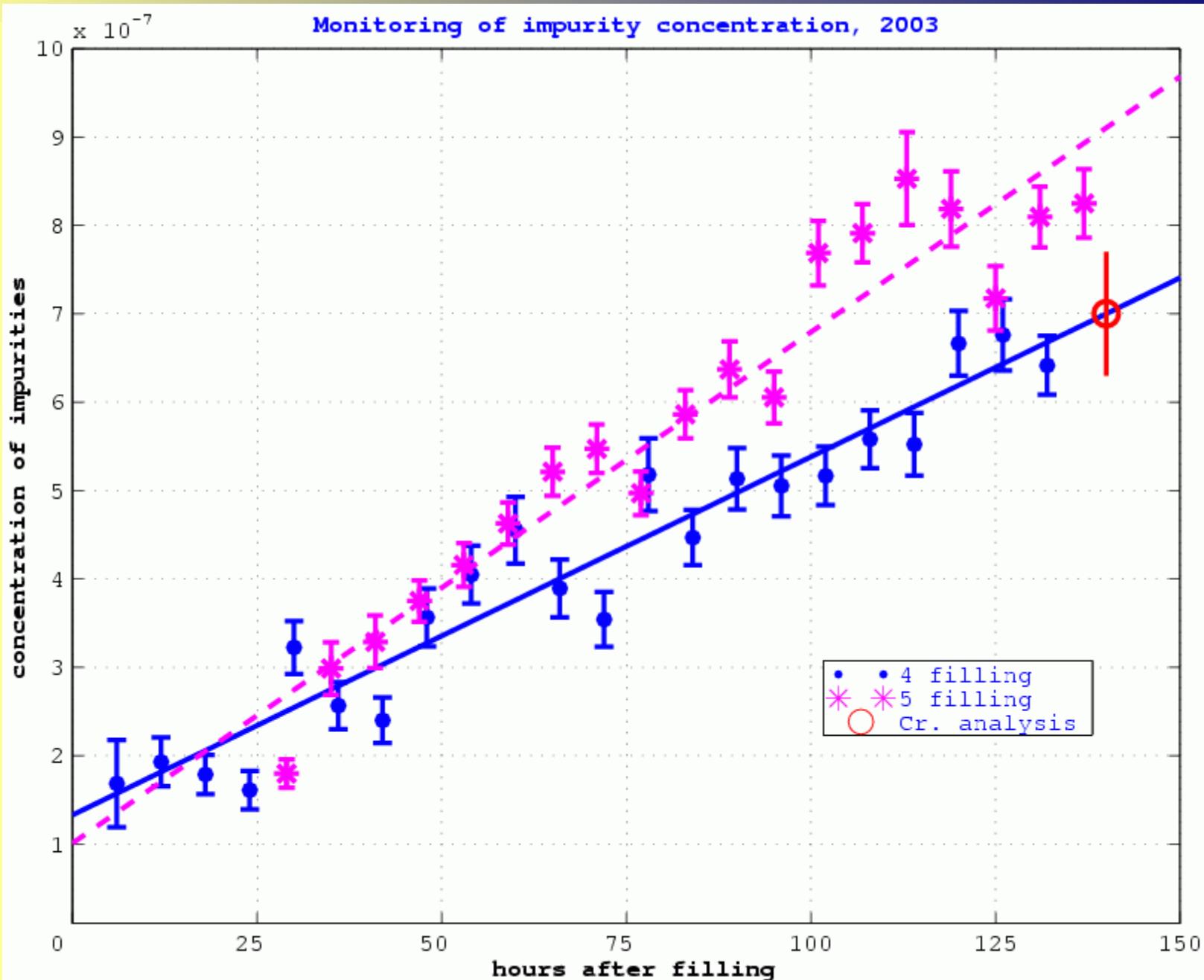


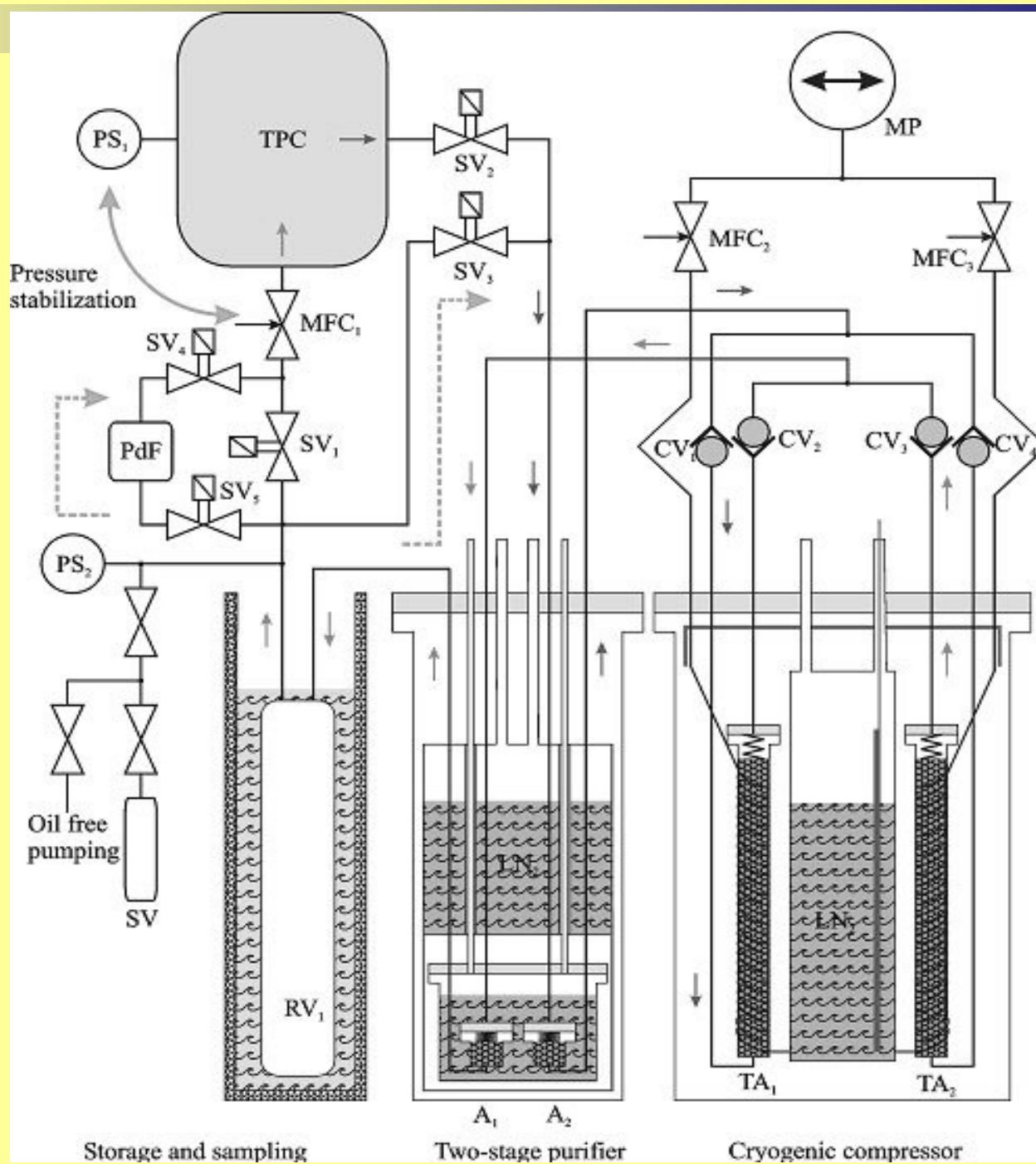
The signal on TPC anode wires from μ -e decay event

μ^- RUN=17, event=45

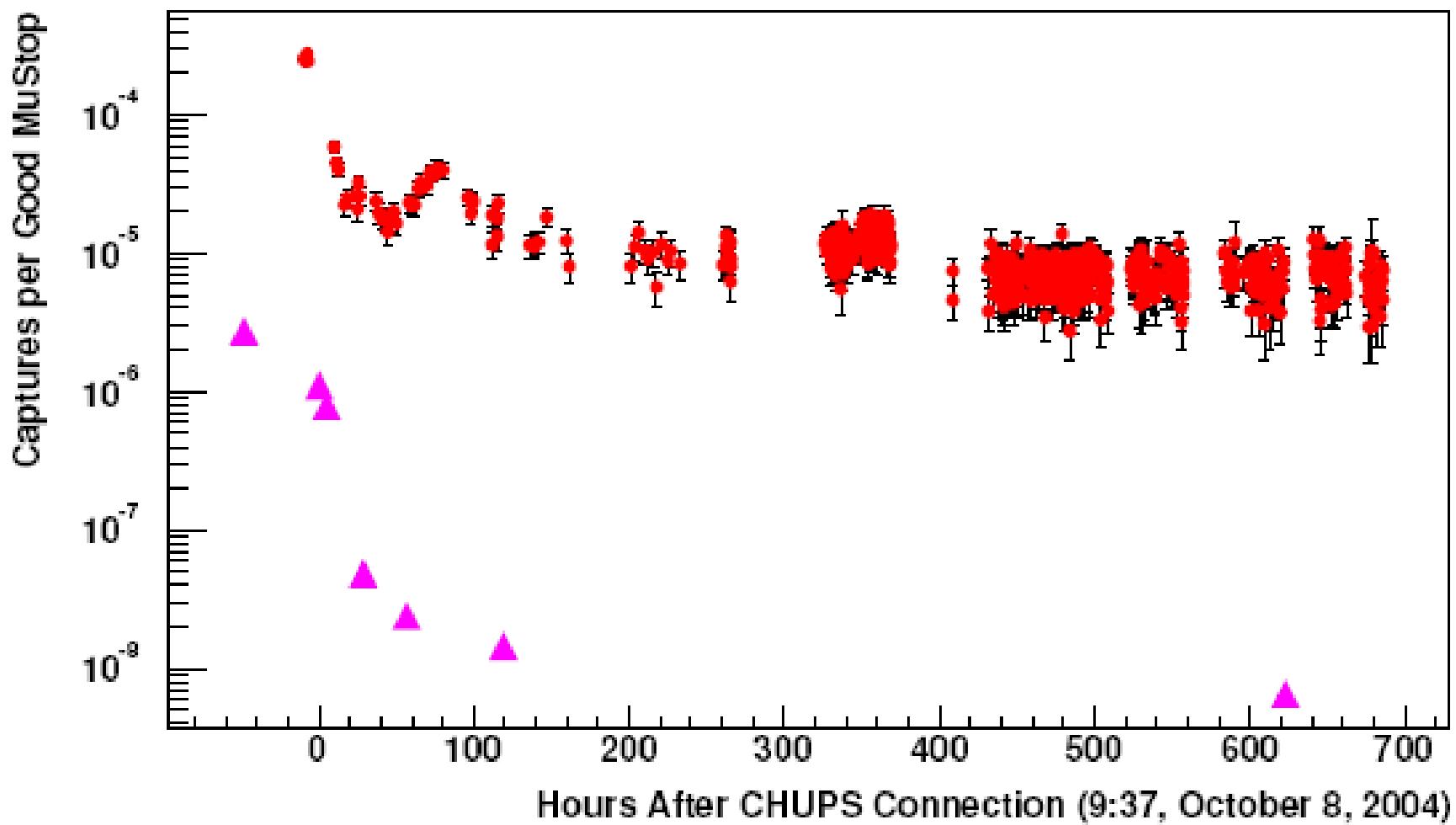


Display of a typical event with μ -capture reaction on impurity

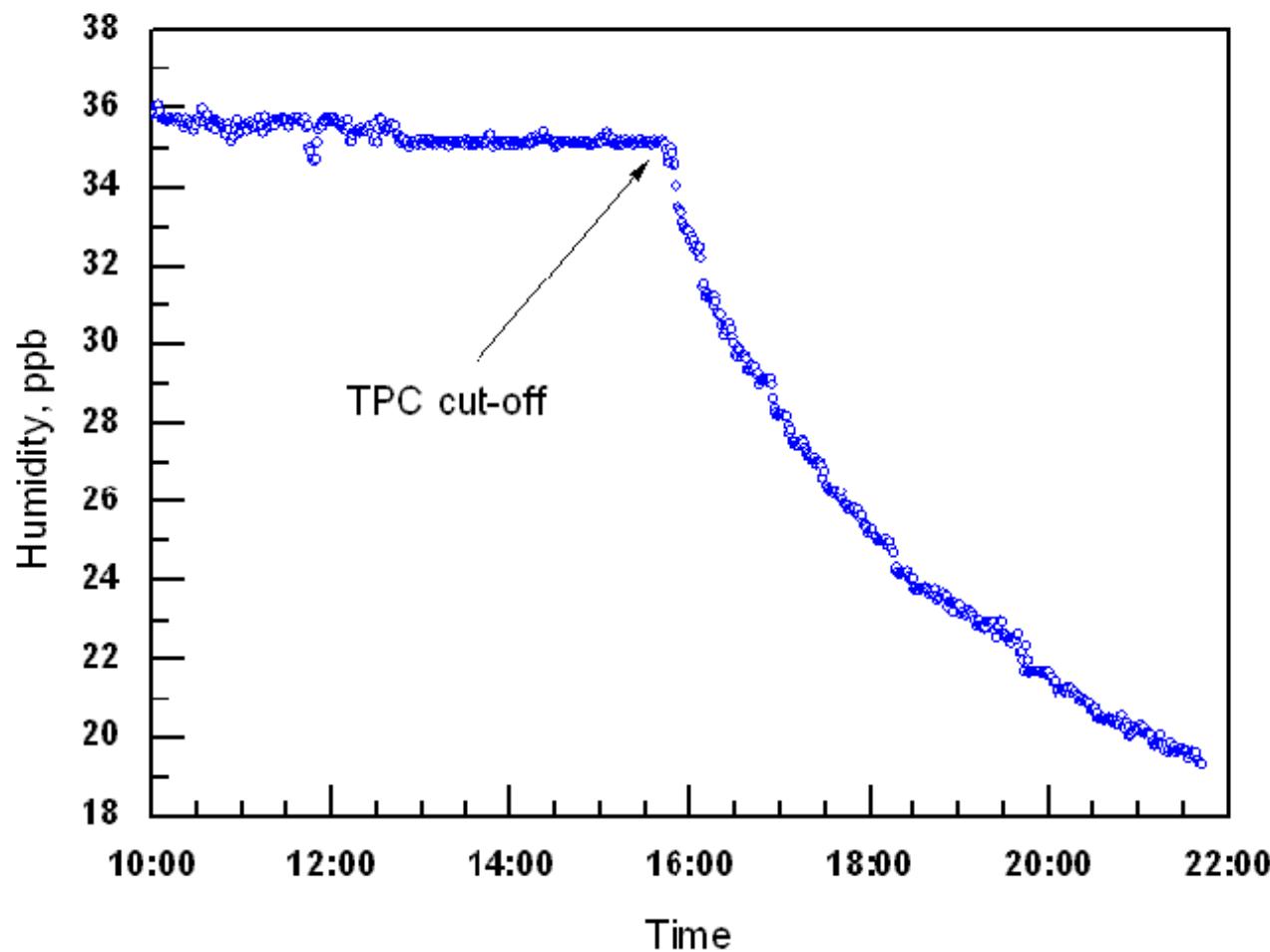


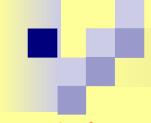


Run8 Gas Impurity vs. Time

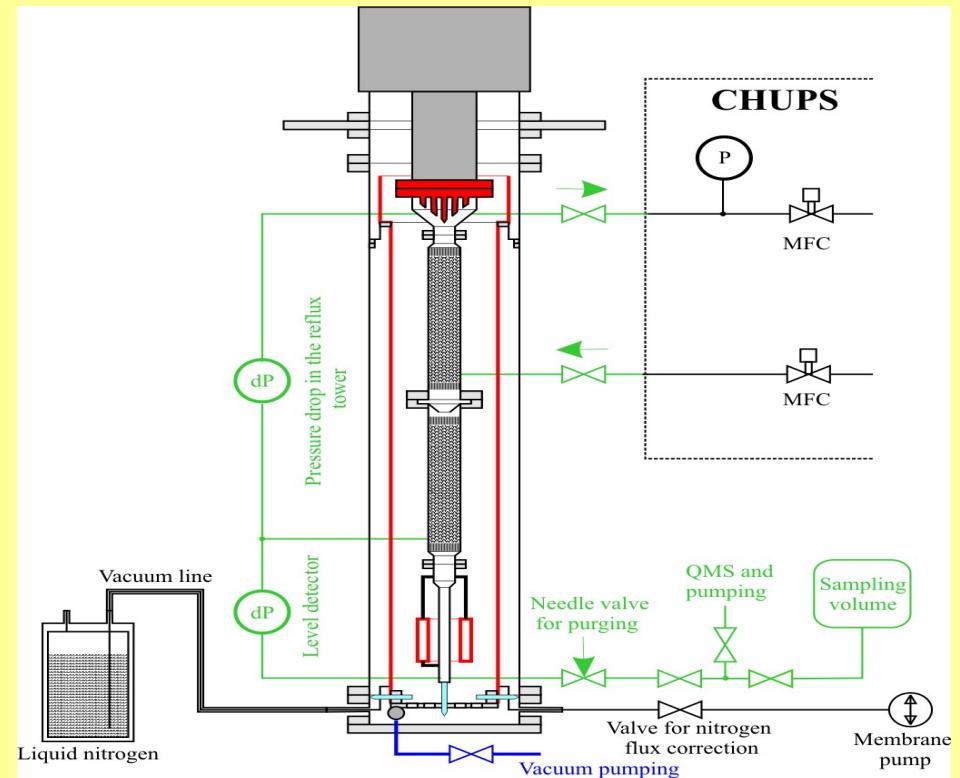


Humidity behaviour during 29.11.2005





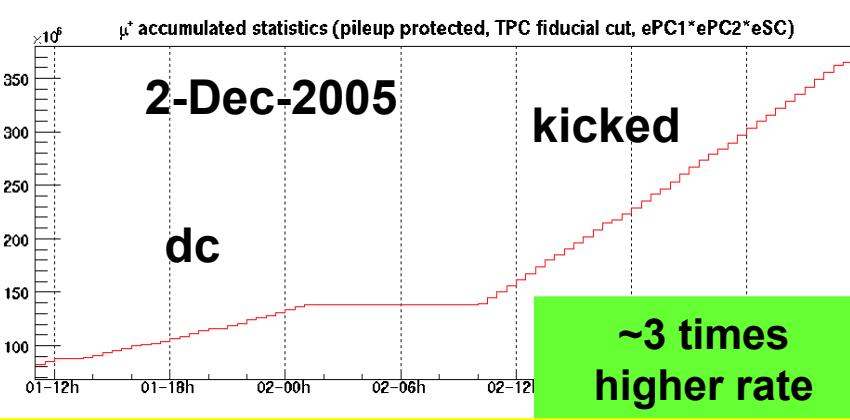
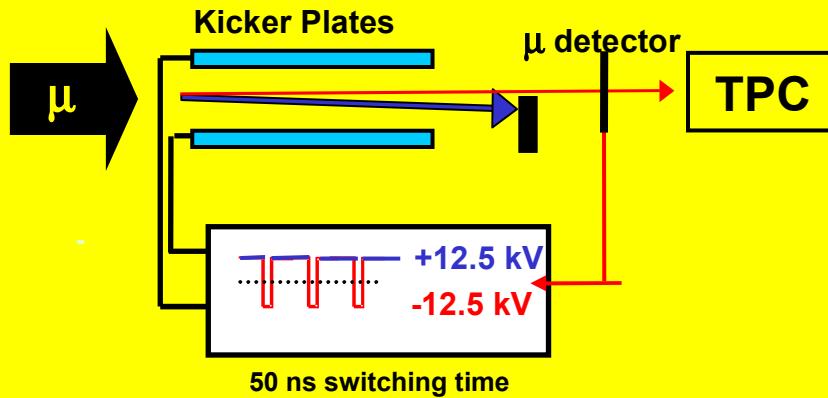
IV. the new protium isotope separation facility: production of ultra-depleted protium



- 1) Cd = 1440 ppb (2004)
- 2) Cd < 60 ppb (2006)
- 3) Cd < 6 ppb (2007)

- Single muon requirement (to prevent systematics from pile-up)
- limits accepted μ rate to ~ 7 kHz,
- while PSI beam can provide ~ 70 kHz

■ Muon-On-Demand concept

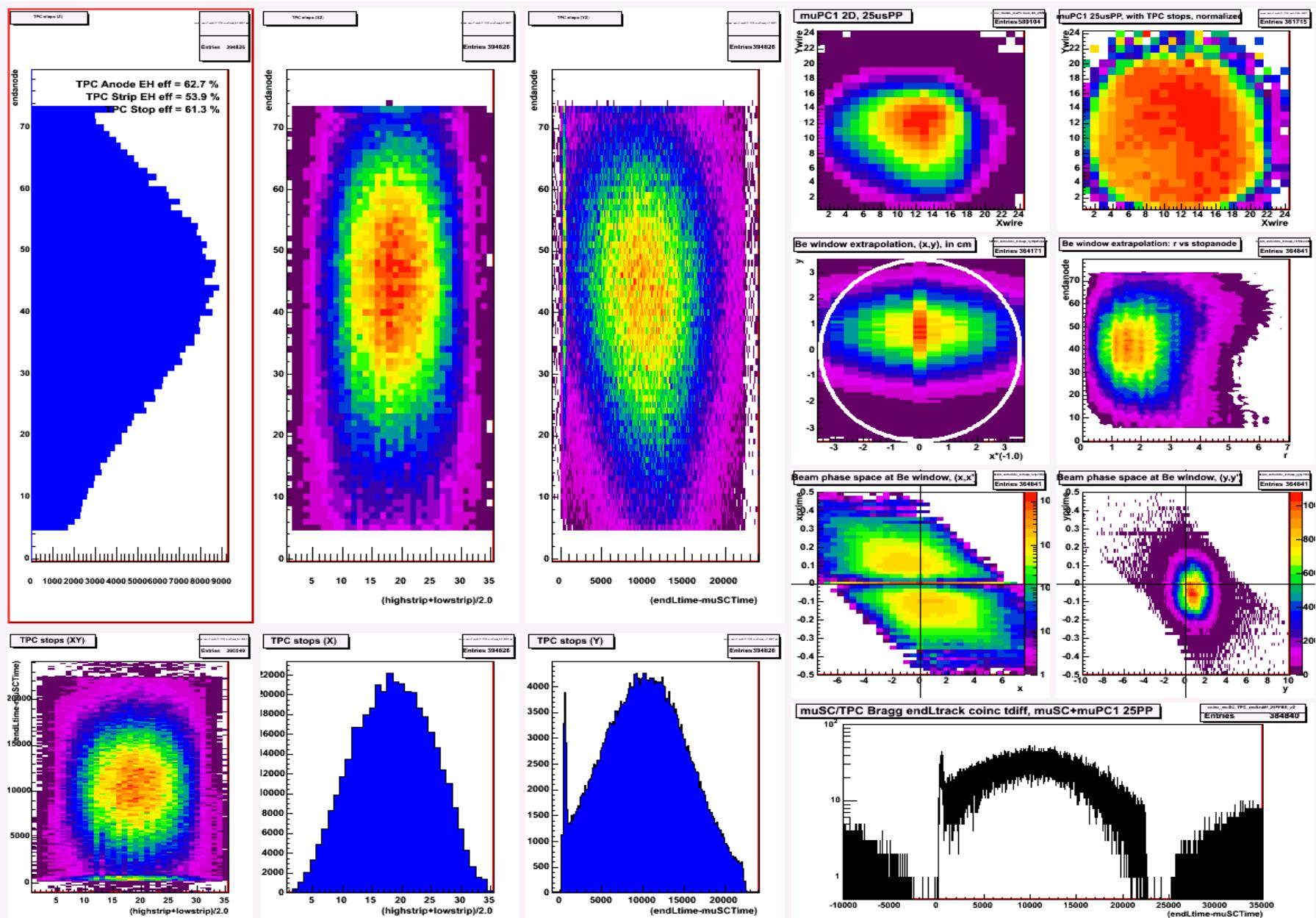


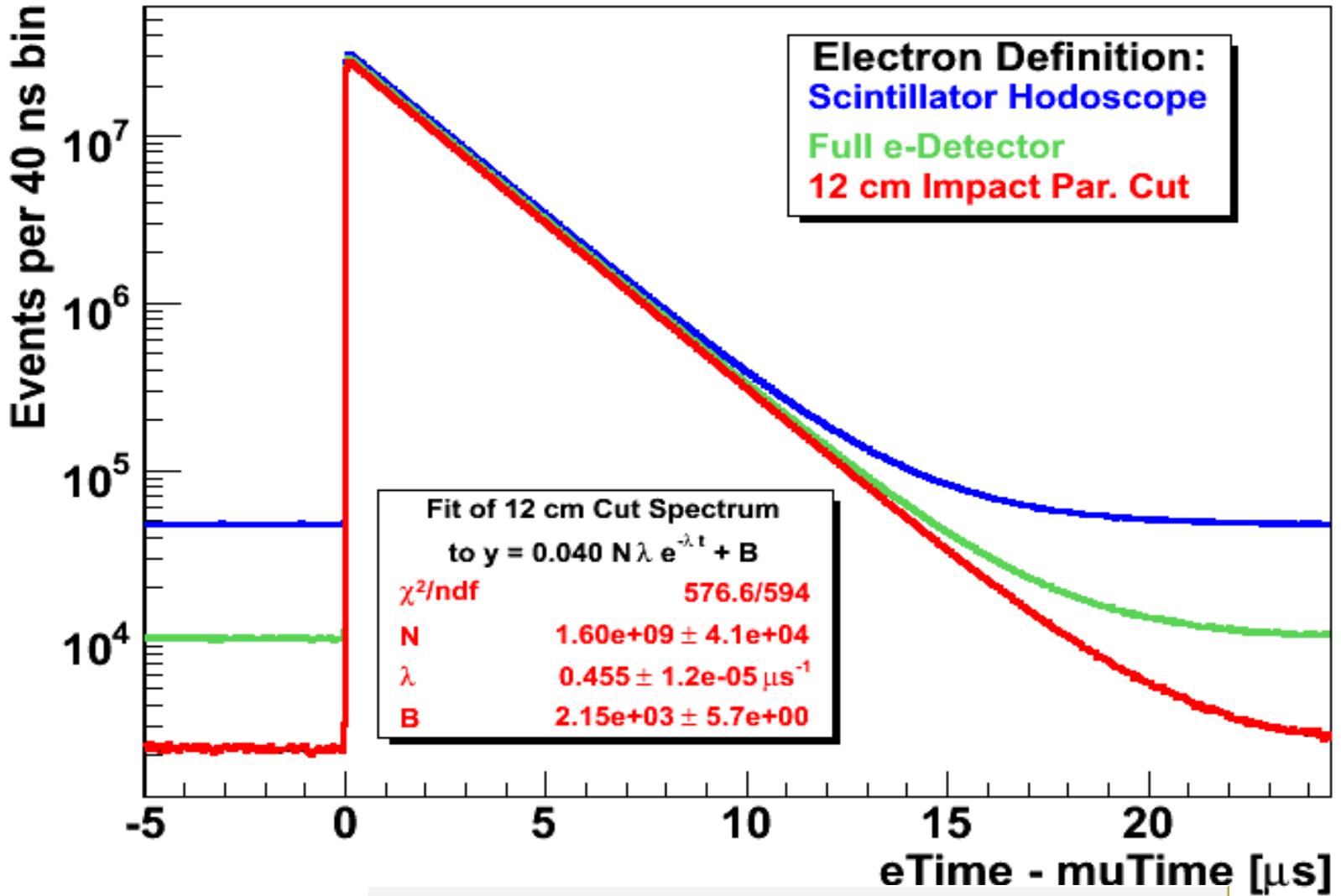
■ Beamlne



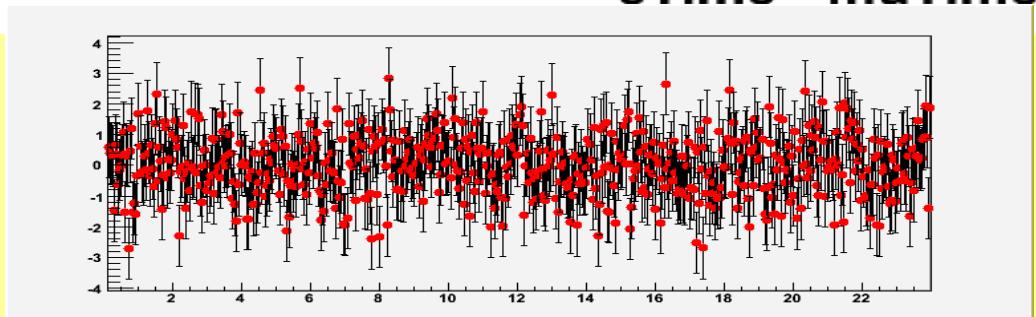
muLan kicker
TRIUMF rf design



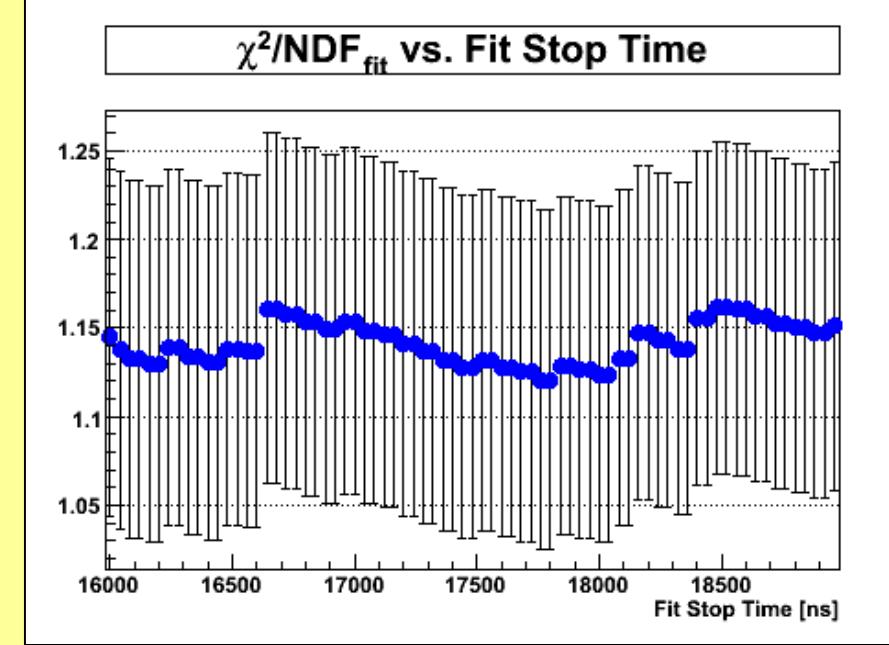
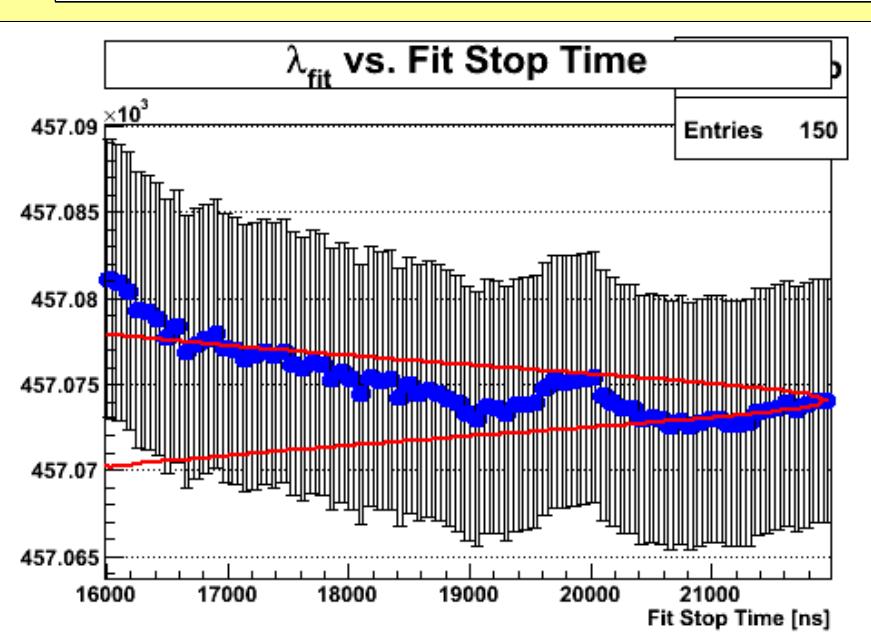
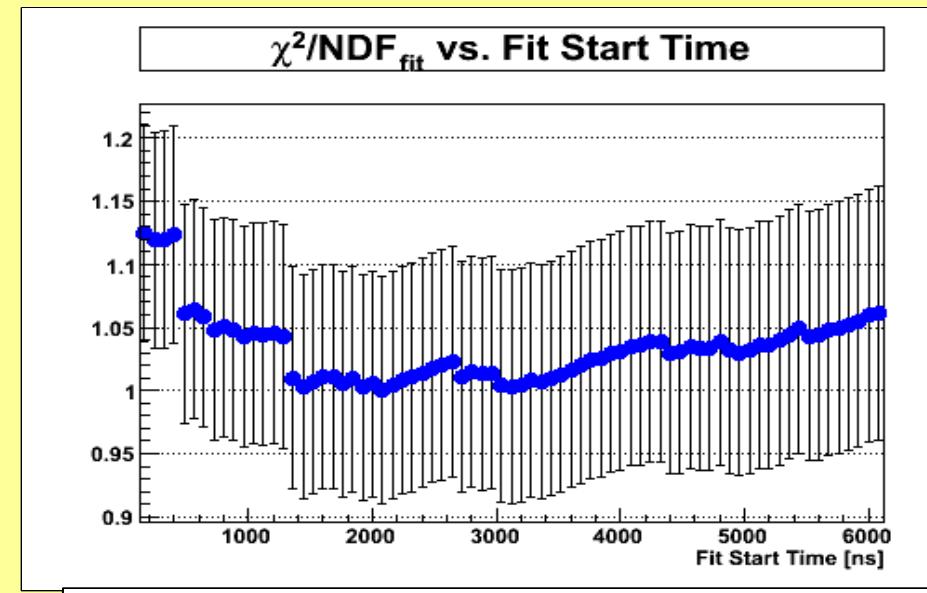
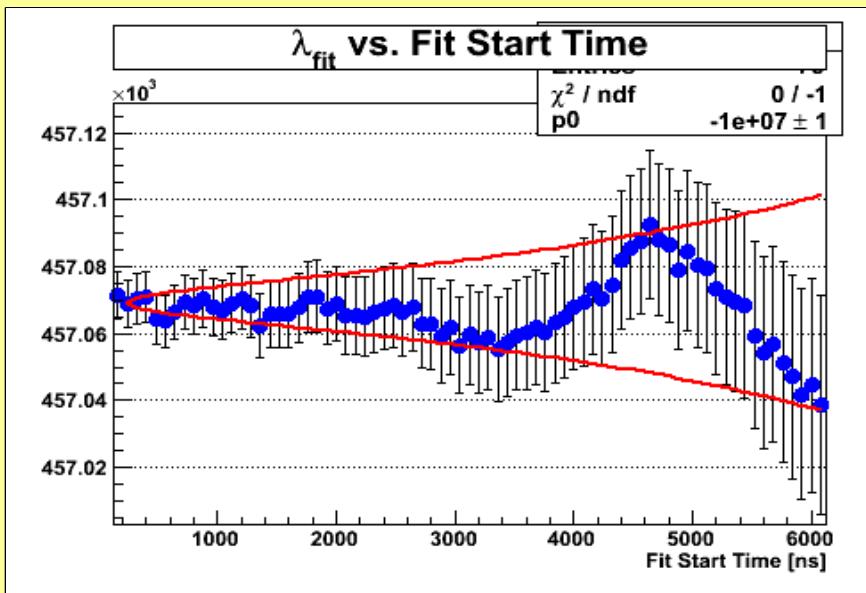




Normalized
residuals



Start and stop-time-scans consistency



Общая набранная статистика

| Год | $\mu^+ (10^9)$ | $\mu^- (10^9)$ | Cd(ppb) | H ₂ O(ppb) |
|------|----------------|----------------|---------|-----------------------|
| 2004 | 0.2 | 2.0 | ~1400 | ~70 |
| 2005 | 1.4 | 3.5 | ~1400 | 36 |
| 2006 | 1.56 | 8.6 | <60 | 18 |
| 2007 | 5.4 | 6.0 | <6 | 8.7 |
| | 8.56 | 20.1 | | |

Общий объем данных за 2004-2007 гг. ~ 100 ТВ

TABLE: Applied corrections and systematic errors.

| Effect | Corrections and uncertainties [s-1] | |
|------------------------------------|-------------------------------------|--------------|
| | R06 | R07 |
| Z > 1 impurities | 7.8 + - 1.9 | 4.5 + - 0.9 |
| mu-p scatter removal | 12.4 + - 3.2 | 7.2 + - 1.3 |
| mu-p diffusion | 3.1 + - 0.1 | 3.0 + - 0.1 |
| mu-d diffusion | + - 0.7 | + - 0.1 |
| Fiducial volume cut | + - 3.0 | + - 3.0 |
| Entrance counter ineff. | + - 0.5 | + - 0.5 |
| Electron track def. | + - 1.8 | + - 1.8 |
| Total corr. λ_{μ^-} | 23.3 + - 5.2 | 14.7 + - 3.9 |
| <hr/> | | |
| mu-p bound state ($D_{\mu p}$) | 12.3 + - 0.0 | 12.3 + - 0.0 |
| ppm̄u states ($D_{pp\bar{\mu}}$) | 17.7 + - 1.9 | 17.7 + - 1.9 |

Результаты анализа данных за 2004-2007 год

$$N_{\mu^-} = 1.2 \times 10^{10}$$

$\lambda_{\mu^-} = 455851.4 \pm 12.5\text{stat} \pm 8.5\text{syst} \text{ s}^{-1}$ (MuCAP 2004).

$\lambda_{\mu^-} = 455857.3 \pm 7.7\text{stat} \pm 5.1\text{syst} \text{ s}^{-1}$ (MuCAP 2006).

$\lambda_{\mu^-} = 455853.1 \pm 8.3\text{stat} \pm 3.9\text{syst} \text{ s}^{-1}$ (MuCAP 2007).

Muon Capture Rate λ_s

$$\lambda_s = \lambda_{\mu^-} - (\lambda_{\mu^+} - D_{\mu p}) + D_{pp\mu}$$

$$D_{\mu p} = 12.3 \text{ s}^{-1} \quad (\mu p \text{ bound state})$$

$$D_{pp\mu} = 17.7 \text{ s}^{-1} \quad (\lambda_{pp\mu} = (1.94 \pm 0.06) \mu\text{s}^{-1})$$

Результаты анализа данных за 2004-2007 год

$$\lambda_{\mu^+} = 455170.05 \pm 0.46 \text{ s}^{-1} (\mu\text{LAN experiment})$$

$$\lambda_{\mu^-} = 455854.9 \pm 5.4\text{stat} \pm 4.7\text{syst} \text{ s}^{-1} (\text{MuCap 2004-2007})$$

$$\Lambda_S^{\text{MuCap}}(\text{aver.}) = 714.9 \pm 5.4\text{stat} \pm 5.3\text{syst} \text{ s}^{-1}$$

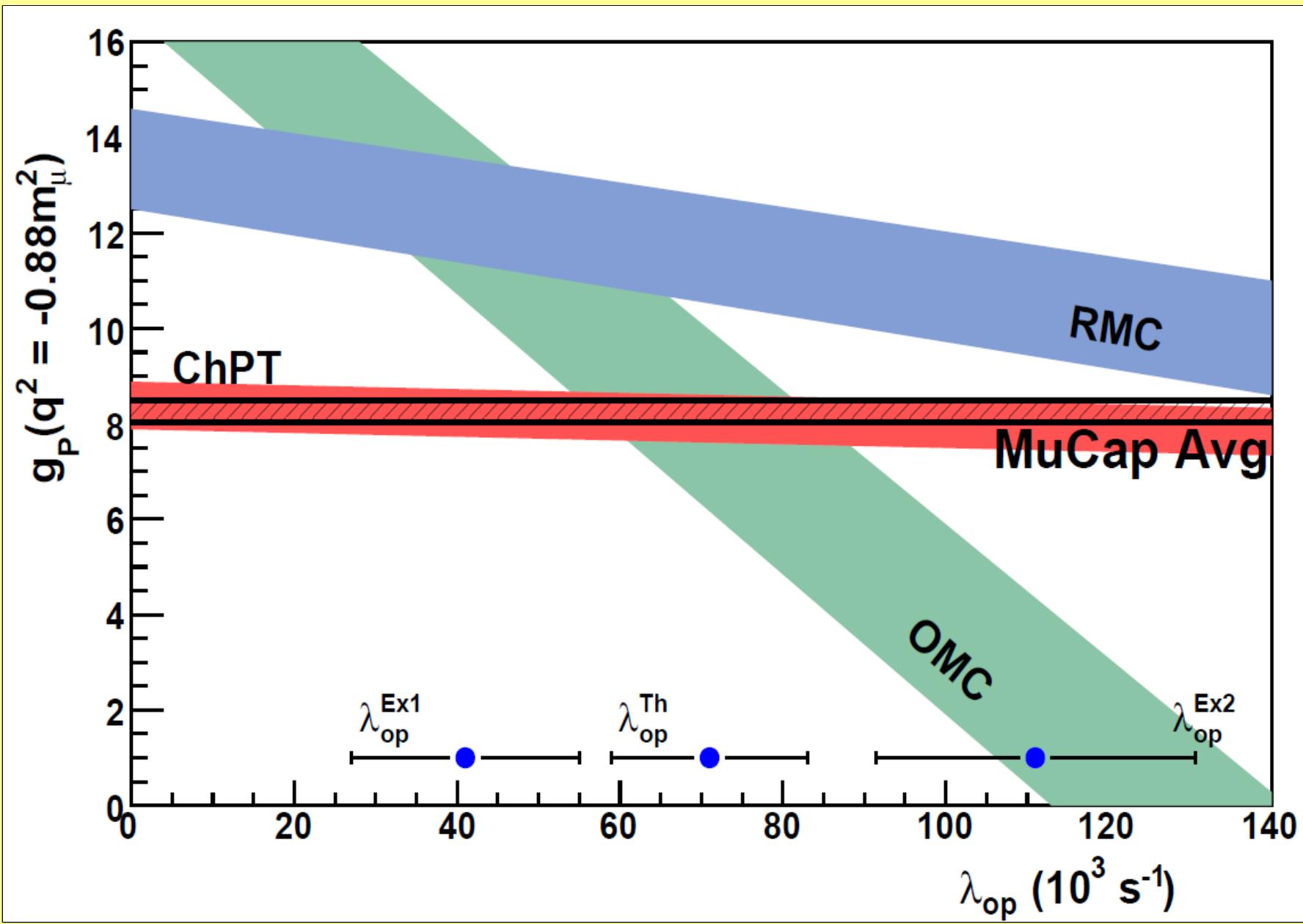
$$\Lambda_S^{\text{Th}} = 693.3 \text{ s}^{-1} (\text{aver.}) + 19.4\text{s}^{-1}(\text{r.c.}) = 712.7 \pm 3.0 \pm 3.0 \text{ s}^{-1}$$

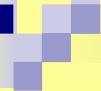
$$g_P^{\text{MuCap}} = g_P^{\text{Th}} - 0.065 \times (\Lambda_S^{\text{MuCap}} - \Lambda_S^{\text{Th}})$$

$$g_P^{\text{MuCap}} = 8.06 \pm 0.48(\text{exp}) \pm 0.28(\text{th})$$

$$g_P^{\text{Th}} = 8.2 \pm 0.2 (2.8\%)$$

Precise and unambiguous MuCap result solves longstanding puzzle





Earlier, in 1998, we have studied the muon capture on ${}^3\text{He}$. The muon capture rate in the channel $\mu^- + {}^3\text{He} \rightarrow {}^3\text{H} + \nu_\mu$ was measured with high precision :

$$\Lambda_c = 1496.0 \pm 4.0 \text{ s}^{-1} \text{ (0.3%).}$$

This result have been used in some theoretical analyses :

L.E. Marcucci et al. (2012) [1] and D. Gazit(2009) [2]

for deriving the Λ_c and the proton's pseudoscalar form factor g_p .

$$\Lambda_c = 1494 \pm 21 \text{ s}^{-1} \text{ [1] and } \Lambda_c = 1499 \pm 12 \text{ s}^{-1} \text{ ([2].}$$

$$g_p = 8.13 \pm 0.6 \text{ [2]}$$



MuCap collaboration

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University of California, Berkeley (UCB and LBNL), USA

University of Illinois at Urbana-Champaign (UIUC), USA

Université Catholique de Louvain, Belgium

TU München, Garching, Germany

University of Kentucky, Lexington, USA

Boston University, USA